

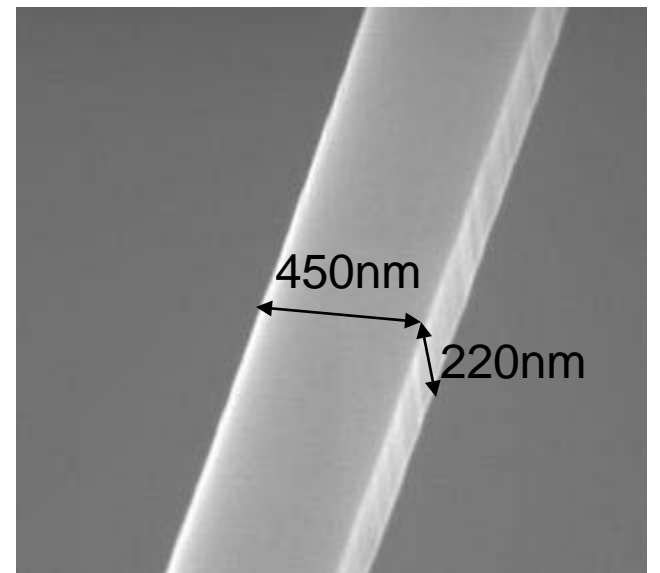
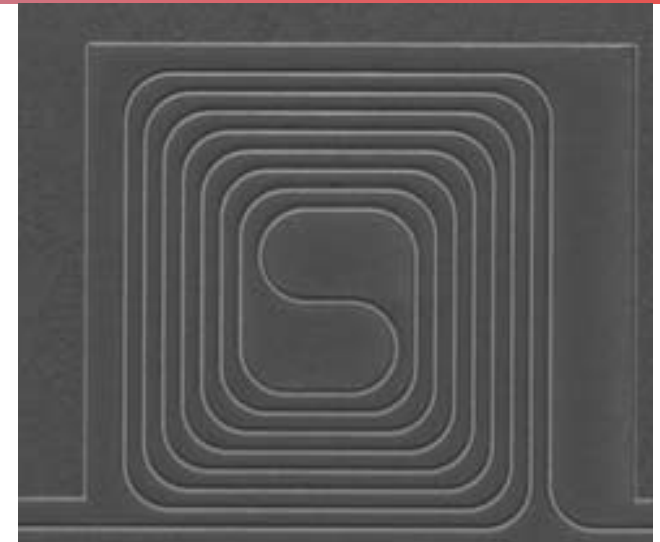
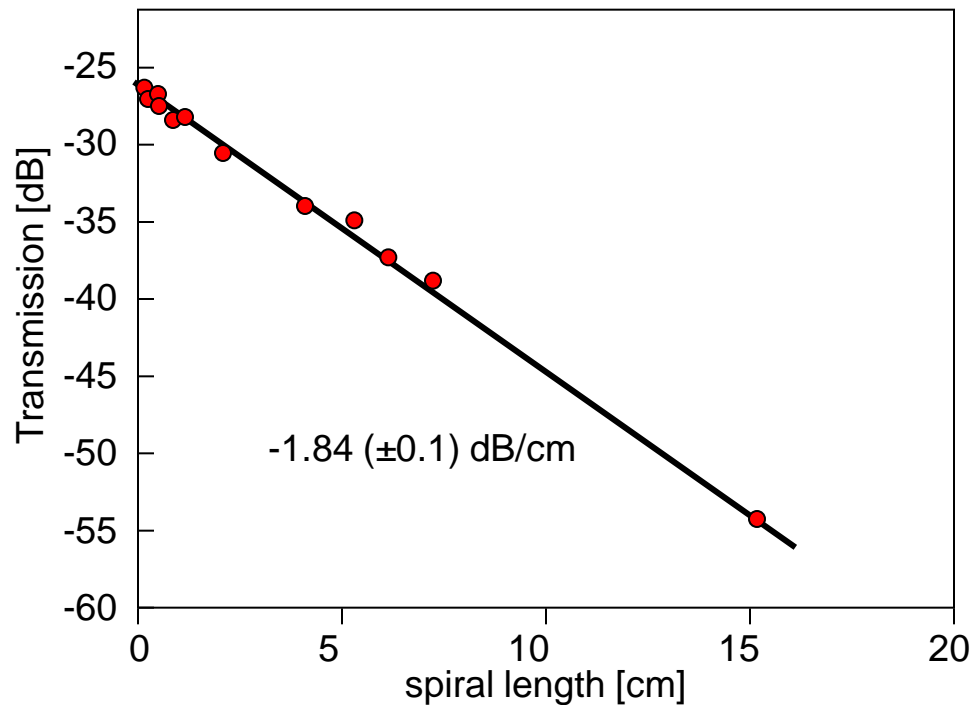


lecture: *Silicon Photonic Devices*

Prepared by *Dries Van Thourhout*
Ghent University - IMEC

- Outline
 - **The Straight Waveguide**
 - The Waveguide Bend
 - The Directional Coupler
 - Star coupler
 - The Multimode Interference Coupler
 - The Y-junction
 - The Mach–Zehnder Interferometer
 - The AWG

- Etched wire in silicon
 - 450 x 220 nm²
 - straight loss: 1.84dB/cm (1.55um wavelength)



- Propagation loss in waveguides
 - Interaction light-material → **absorption**
 - Imperfections in the waveguide → **scattering**
 - spatial refractive index variations
 - rough interfaces
 - Imperfect guiding → **radiation**

→ Guided optical power decreases:

$$P(z) = P_0 e^{-\alpha z}$$

for a uniform distribution of the losses

Losses by absorption

- Semiconductors:
 - photon $h\nu > E_{\text{bandgap}}$: creation of e^-h^+ pair
 - wanted in detectors
 - unwanted in waveguides
 - Choose a material with sufficiently large E_{bandgap}
 - Silicon: no loss if $\lambda > 1.1\mu\text{m}$
- Dielectrics: absorption by molecular and atomic energy transitions
 - Silicon waveguides: absorption by surface states has strong impact
 - Solution: surface passivation Painter e.a.
- Free carriers (metals and semiconductors): carriers absorb energy from electric field Soref e.a. , JQE 22, p. 873 (1986)

Scattering losses

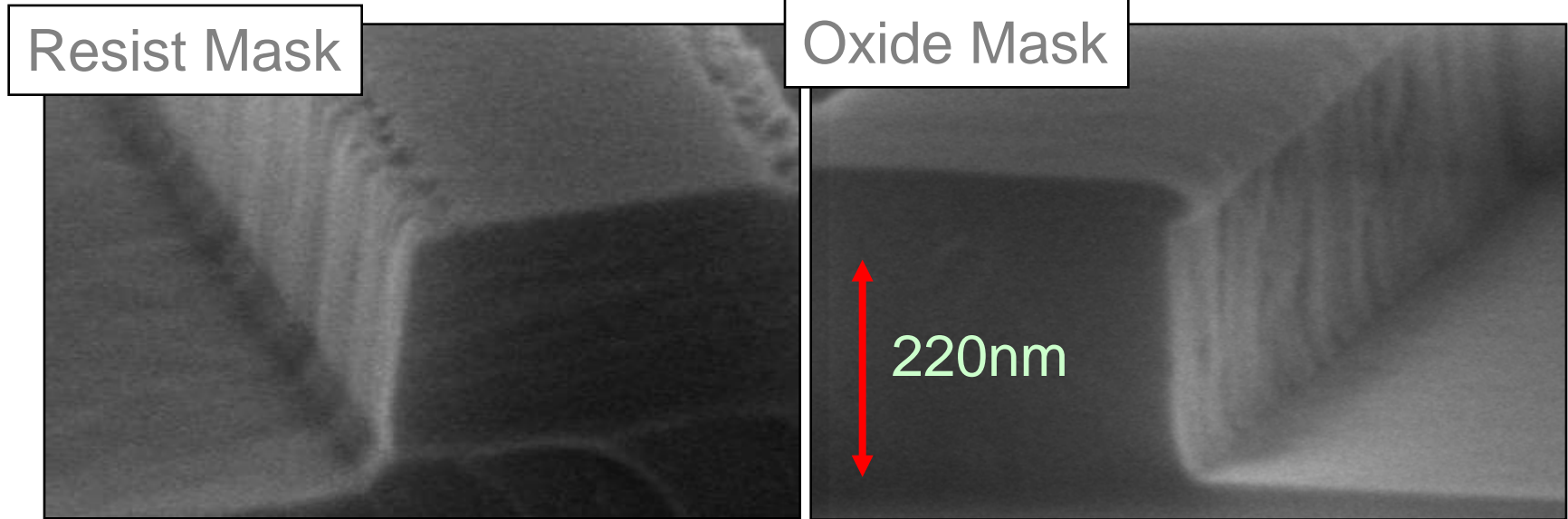
- Volumetric scattering: by spatial refractive index variations
 - Less relevant for silicon waveguides
- Surface scattering (dominant in waveguides):
roughness of the interfaces
 - etched sidewalls of the waveguide
 - interface between grown layers

- Scattering losses at interfaces (approximately):

$$\alpha = \alpha_{\text{scat}} \frac{(\Delta n)^2 E_s^2}{P}$$

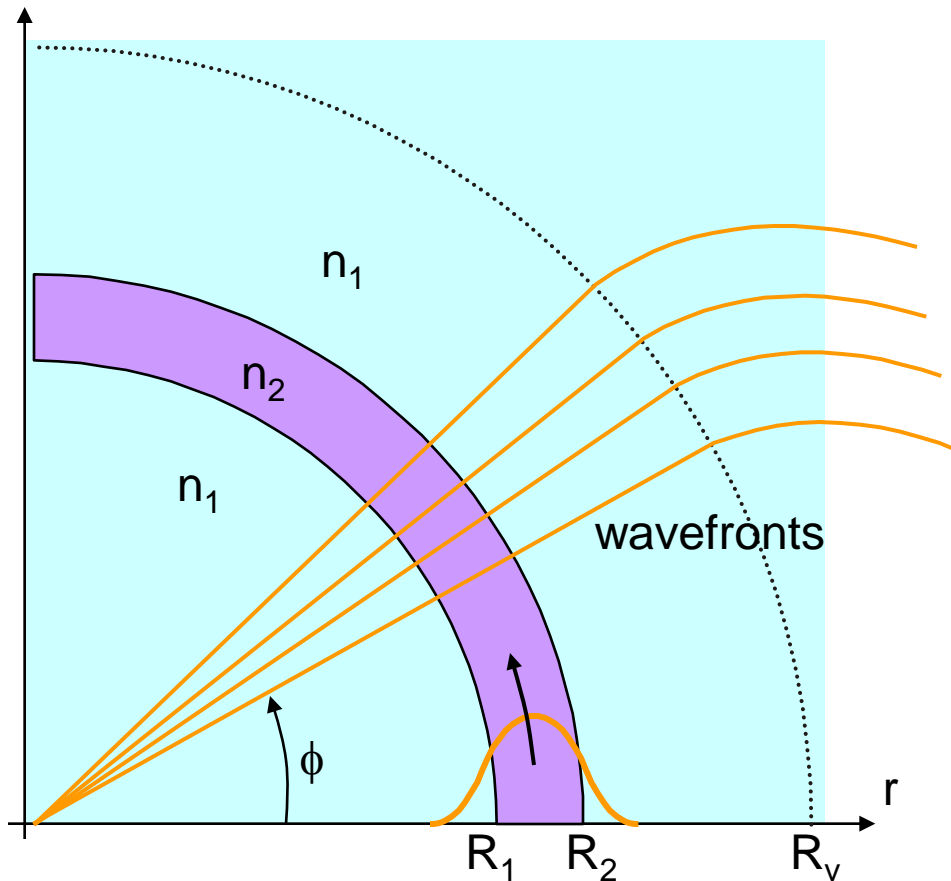
with P the optical power and E_s the field on the interface

- α_{scat} to determine empirically



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- Bend waveguides show a fundamental loss:



- Wavefront revolves around center
- Group velocity of wavefront cannot exceed c/n
- bending of wavefront
- radiation

Radiation losses increase with smaller bend radii

↑↓ **tradeoff**

Smaller bend radius needed for larger-scale integration

- Calculate propagation losses:

- Two-dimensional waveguide (cylinder coordinates)

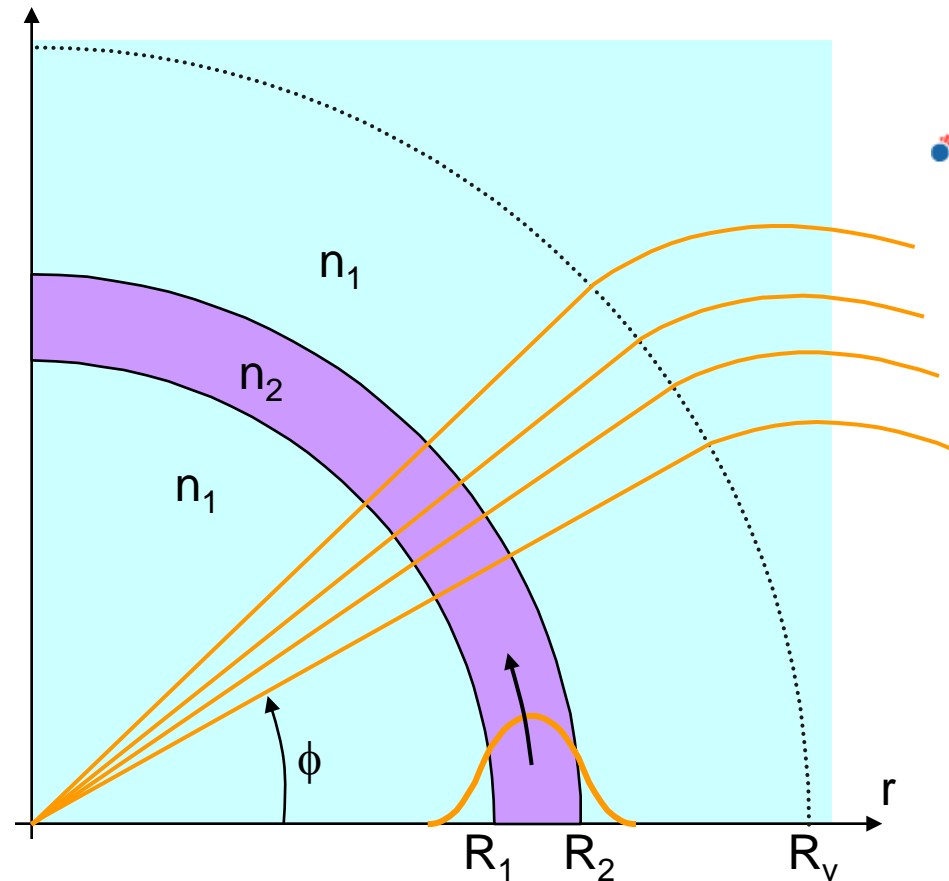
- Helmholtz equation:

$$\left(\frac{\partial^2}{\partial r^2} + \frac{1}{r} \frac{\partial}{\partial r} + \frac{1}{r^2} \frac{\partial^2}{\partial \phi^2} + k_0^2 n^2(r) \right) \Psi(r, \phi) = 0$$

Fill-in solution: $\Psi(r, \phi) = \psi(r)\Phi(\phi)$

- $\psi(r)$: mode profile

- $\Phi(\phi)$: propagation



- Wave equation:

$$\underbrace{\left(\frac{r^2}{\psi(r)} \frac{\partial^2}{\partial r^2} + \frac{r}{\psi(r)} \frac{\partial}{\partial r} + r^2 k_0^2 n^2(r) \right)}_{\text{function of } r} \psi(r) = - \underbrace{\frac{1}{\Phi(\varphi)} \frac{\partial^2 \Phi(\varphi)}{\partial \varphi^2}}_{\text{function of } \varphi} \longrightarrow = \text{cst}$$

- Right side:

$$\frac{1}{\Phi(\varphi)} \frac{\partial^2 \Phi(\varphi)}{\partial \varphi^2} + \beta_\varphi^2 = 0$$

- Generic solution $\Phi(\varphi) = C e^{\pm j \beta_\varphi \varphi}$

→ Phase fronts turn with bend

- Left side of the wave equation:

$$\left(\frac{r^2}{\psi(r)} \frac{\partial^2}{\partial r^2} + \frac{r}{\psi(r)} \frac{\partial}{\partial r} + r^2 k_0^2 n^2(r) \right) \psi(r) - \beta_\phi^2 = 0$$

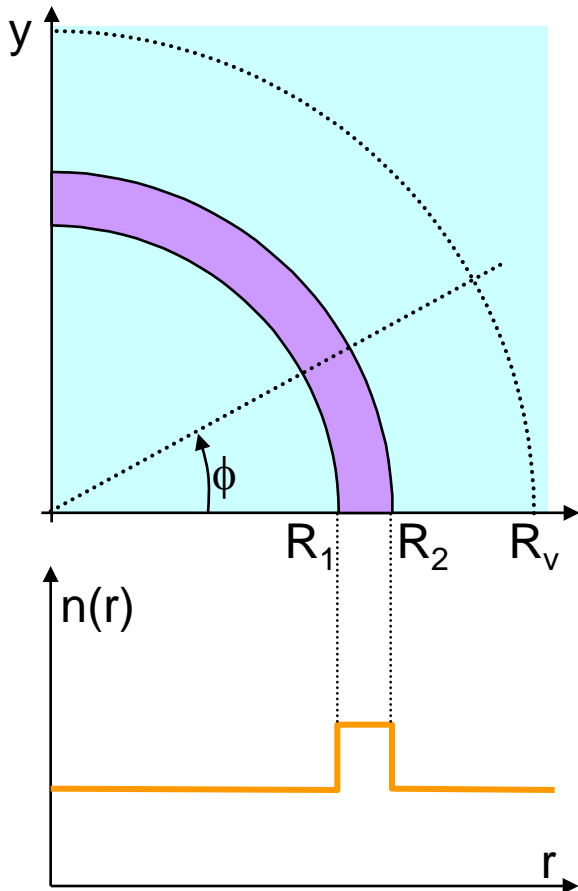
Substitution: $r = R_t e^{u/R_t} \rightarrow u = R_t \ln \frac{r}{R_t}$

$$\left[\frac{\partial^2}{\partial u^2} + \left(k_0^2 n_t^2(u) - \beta_t^2 \right) \right] \psi(u) = 0$$

with $n_t(u) = n(u) e^{u/R_t}$ and $\beta_t = \frac{\beta_\phi}{R_t}$

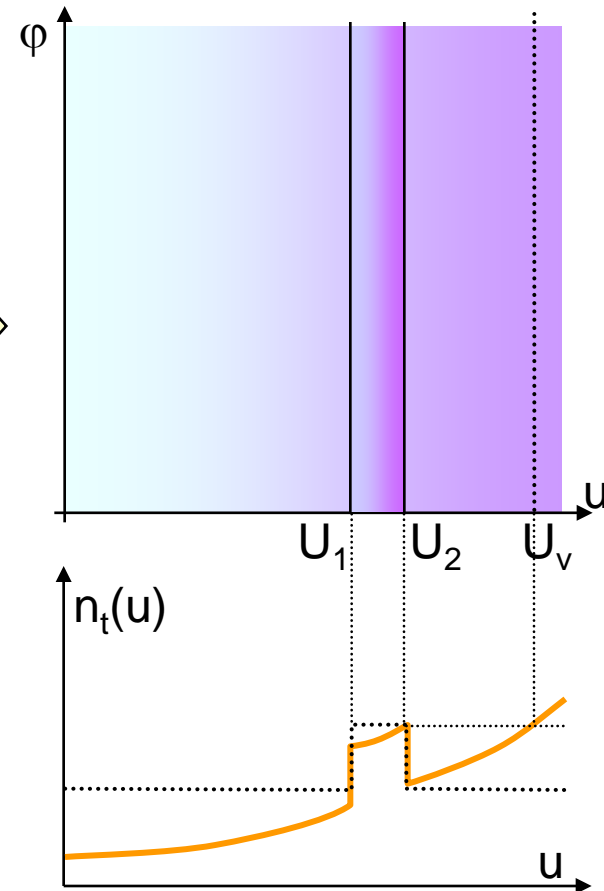
- Same Helmholtz equation in (u, ϕ) problem as in cartesian coordinates with a different refractive index profile $n_t(u)$!!!

- Coordinates (x,y)



- Coordinates (u,φ)

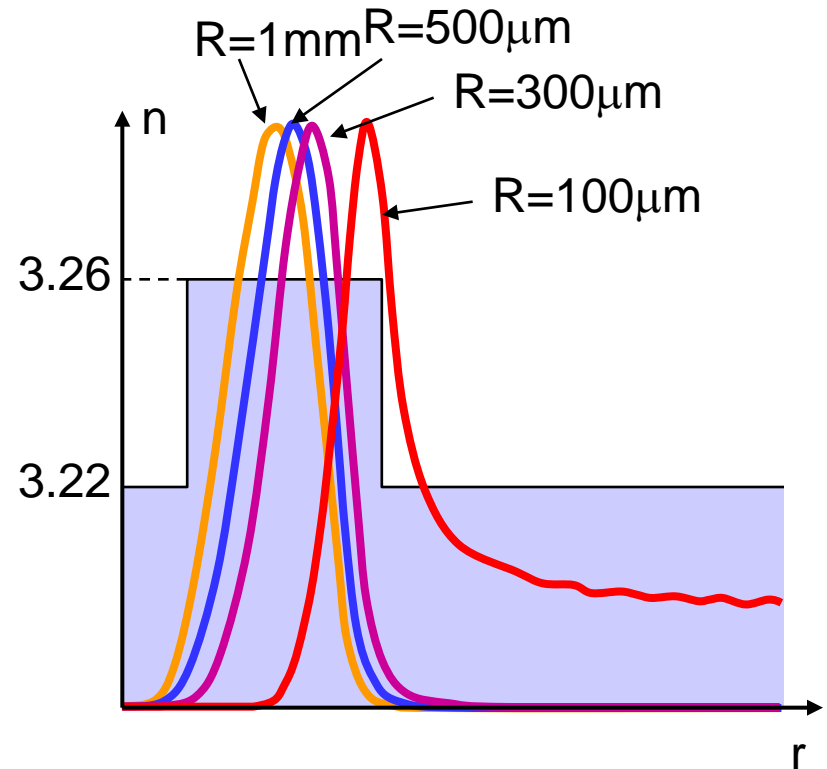
$$r = R_t e^{u/R_t}$$



- Waveguide mode and losses can easily be calculated using standard slab solvers and the modified refractive index profile

- Modified index profile learns us a lot already :

- Mode mostly guided in region with largest index
 - mode shifts outward
 - mismatch losses at transition between straight and bent waveguide
- “Sharp” bends: mode only on the outside
 - no guiding by inner interface
 - “Whispering Gallery” modes
- Strong field on the outer interface → scattering losses

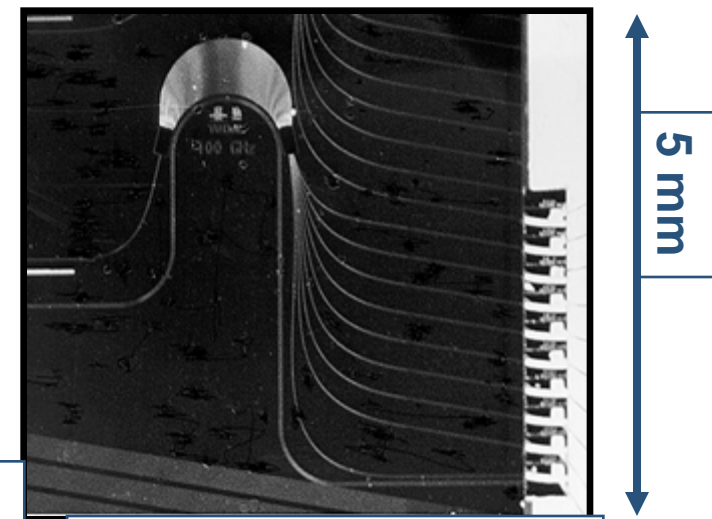


Mode profile calculation using conformal transformation.

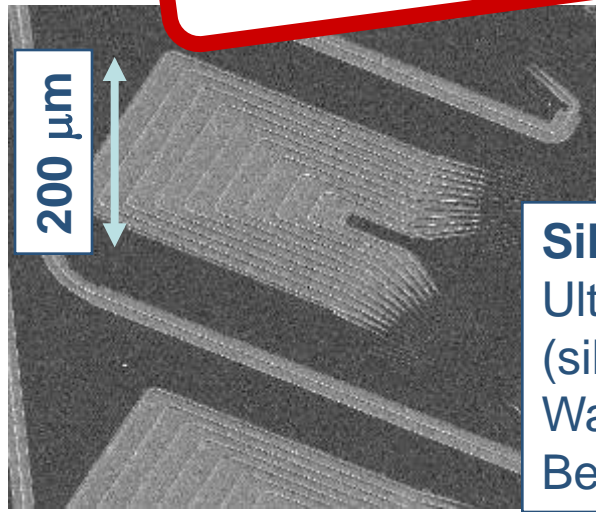


Glass photonic ICs
 Low Contrast - Fiber Matched
 (doped silica vs pure silica)
 Waveguide: $10 \times 10 \mu\text{m}^2$
 Bend Radius $\sim 5 \text{ mm}$

Density $\times 10^6$

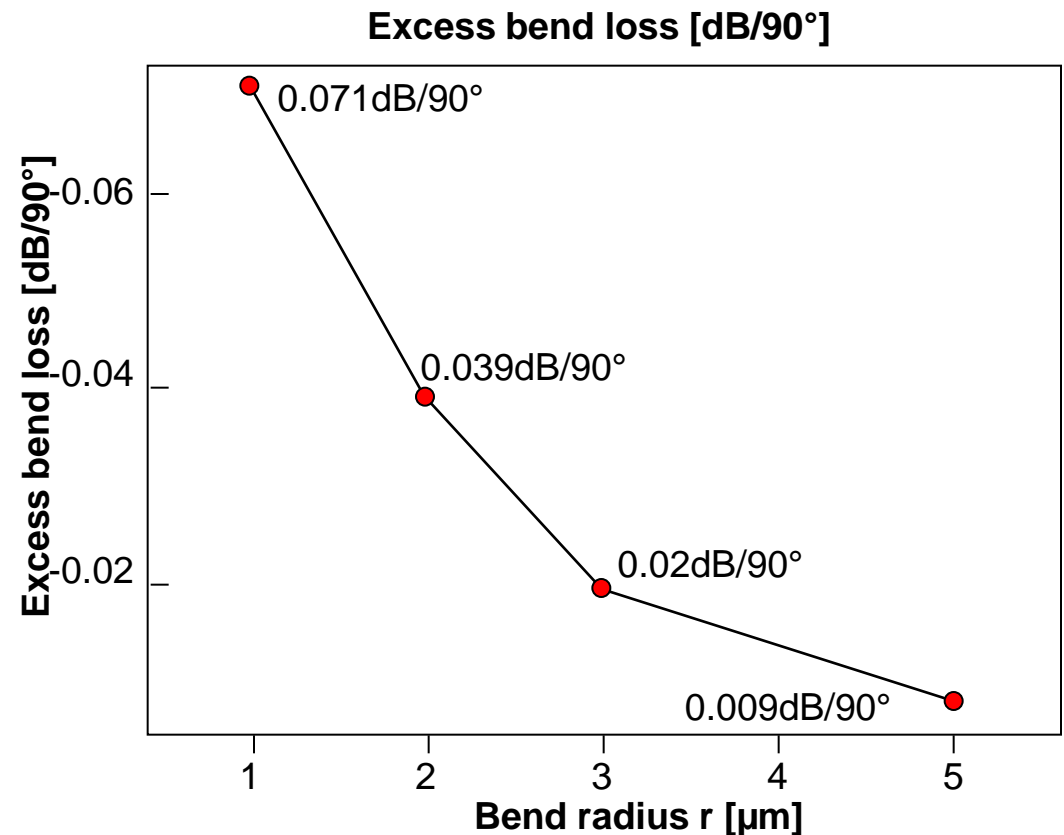
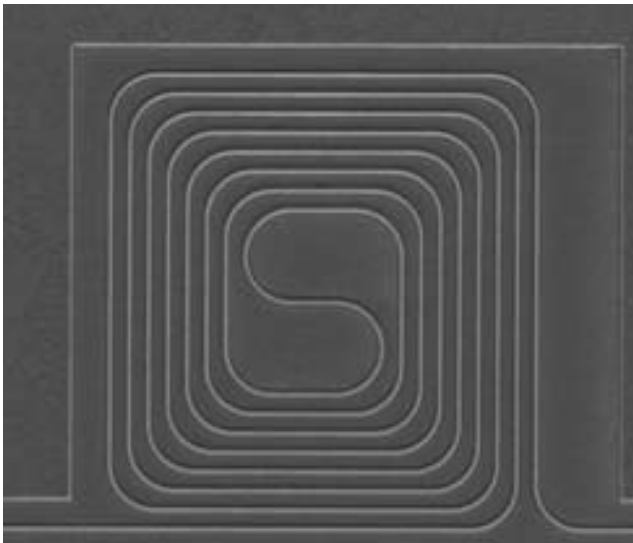


III-V photonic ICs
 Medium Contrast
 (InGaAsP vs InP)
 Waveguide: $2 \times 1 \mu\text{m}^2$
 Bend Radius $\sim 500 \mu\text{m}$

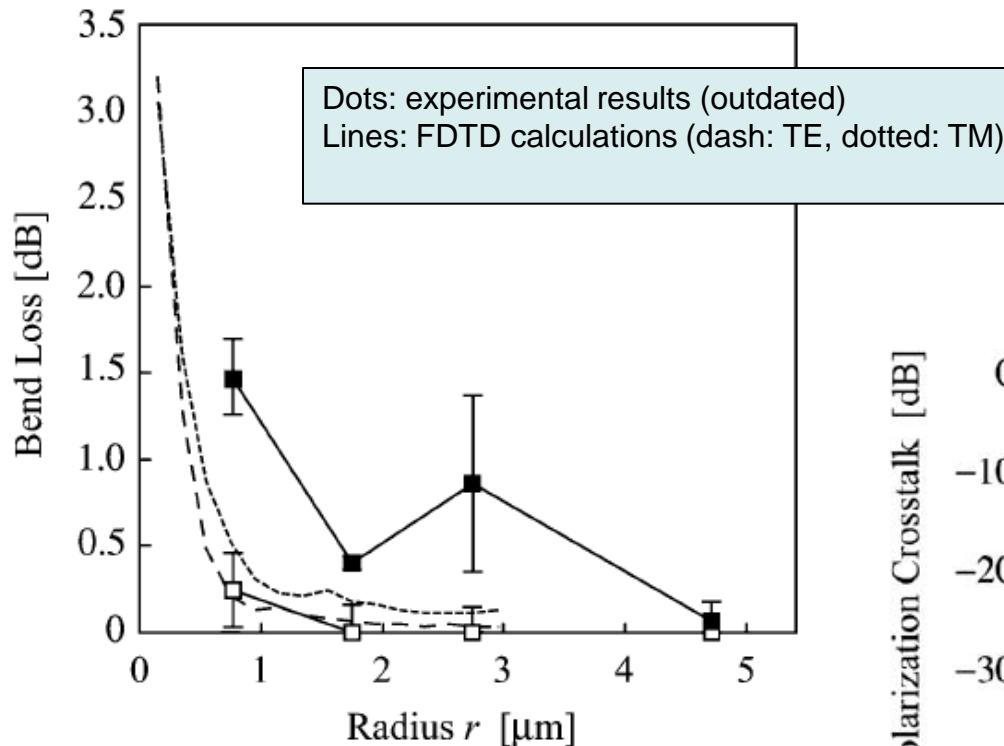


Silicon photonic ICs
 Ultra-high Contrast
 (silicon vs silica)
 Waveguide: $500 \times 200 \text{ nm}^2$
 Bend Radius $< 5 \mu\text{m}$

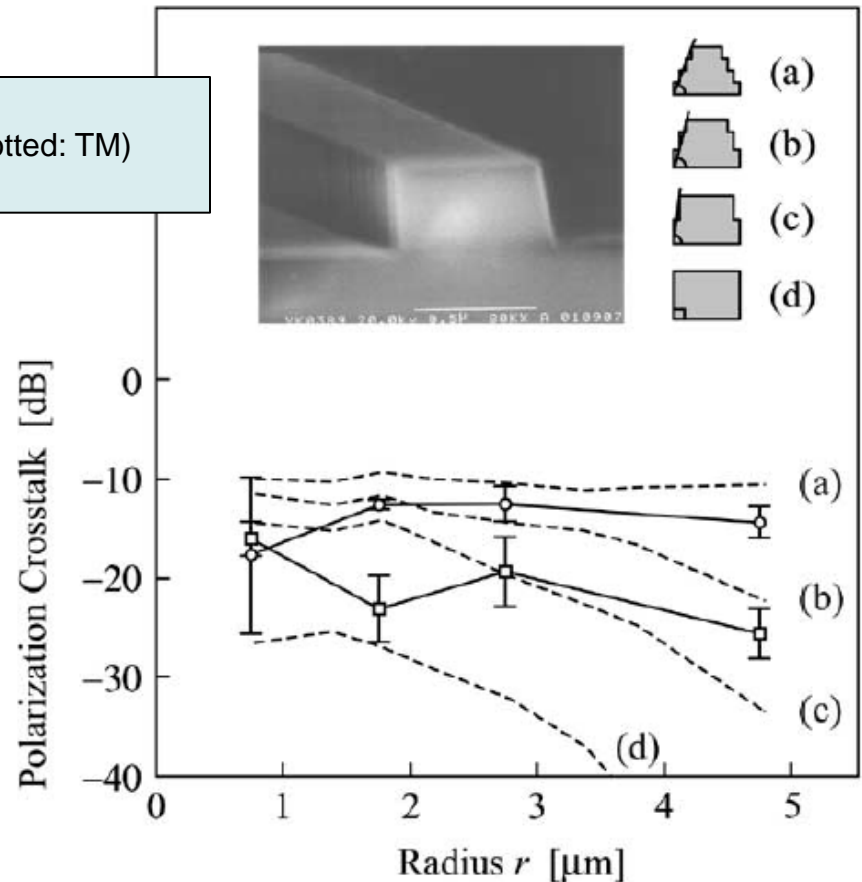
- Bend losses in silicon wires measured from spirals containing several 100s of bends
- Several groups obtained comparable results



- FDTD calculations in line with recent experimental results



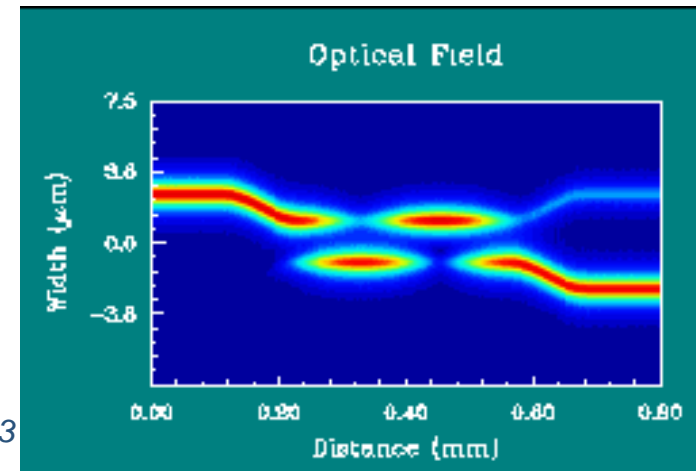
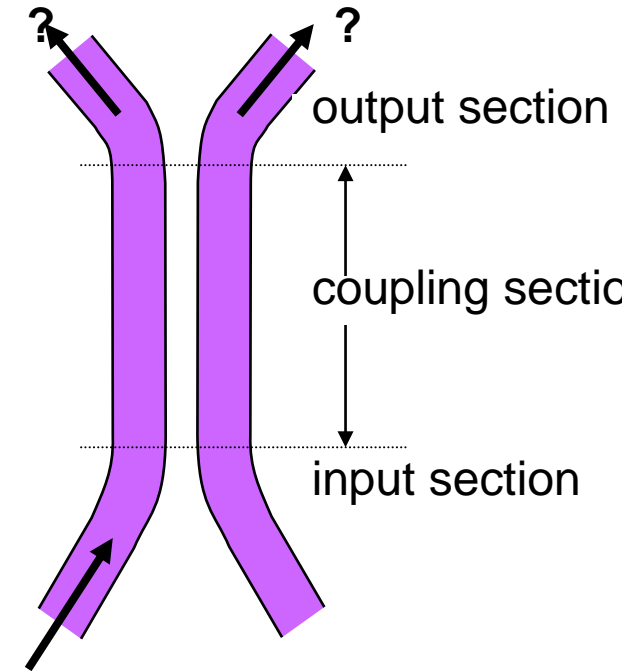
- Bends may introduce unwanted polarization rotation



A. Sakai, JLT 22, pp 520 (2004)

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- Two waveguides close together
 - Evanescent field of first waveguide “feels” second waveguide
 - Gradual coupling of light between both waveguides
- Coupling controlled by length
- Identical waveguides : full coupling
- Otherwise: partial coupling
- Applications: variable splitter, polarization convertor, base component for ring resonator ...



- Coupled waveguides two “supermodes”

- ϕ_+ : symmetric
- ϕ_- : antisymmetric

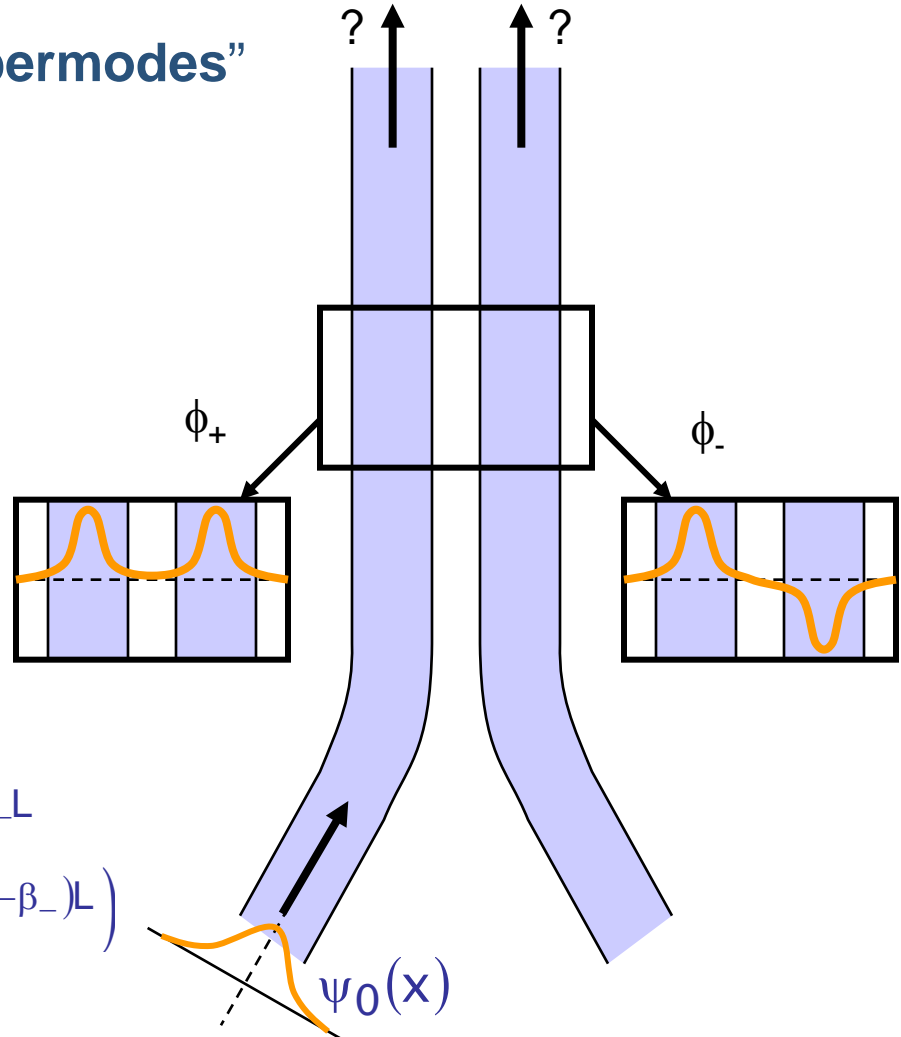
- Field in $z=0$:

$$\Psi(x, z = 0) = \psi_0(x) \approx c_+ \phi_+ + c_- \phi_-$$

$$\text{with } c_+ = c_- = 1/\sqrt{2}$$

- After propagation ($z=L$)

$$\begin{aligned} \Psi(x, z = L) &= c_+ \phi_+ e^{-j\beta_+ L} + c_- \phi_- e^{-j\beta_- L} \\ &= c_+ e^{-j\beta_+ L} \left(\phi_+ + \phi_- e^{+j(\beta_+ - \beta_-)L} \right) \end{aligned}$$



- Total field ($z=L$)

$$\Psi(x, z = L) = c_+ e^{-j\beta_+ L} (\phi_+ + \phi_- e^{+j(\beta_+ - \beta_-)L})$$

- All power in second waveguide when

$$\Psi(x, z = L) = c_+ \phi_+ - c_- \phi_-$$

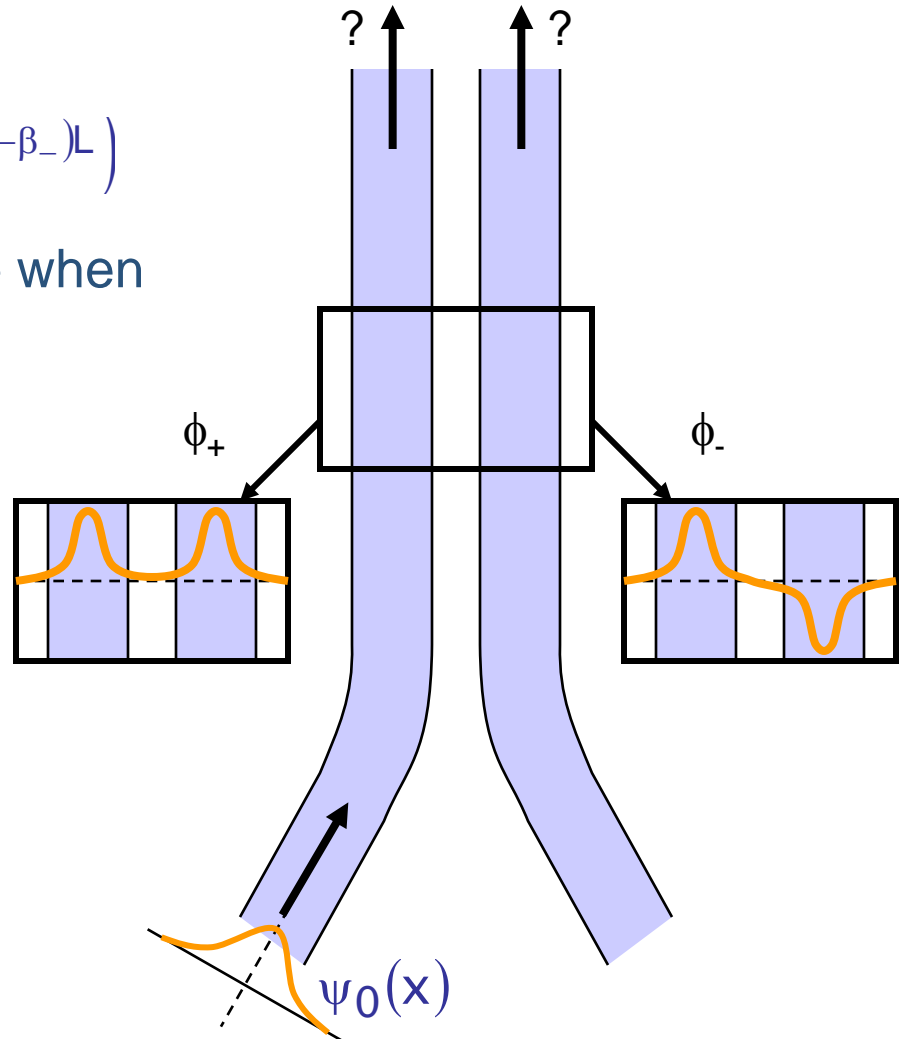
- This is the case when:

$$L = L_c = \frac{\pi}{\beta_+ - \beta_-}$$

(= coupling length)

- Coupling coefficient κ

$$\kappa = \frac{(\beta_+ - \beta_-)}{2}$$



- **Asymmetric coupler**
 - supermodes no longer perfectly symmetric and antisymmetric
 - $C_+ \neq C_-$

- After propagation ($z=L$)

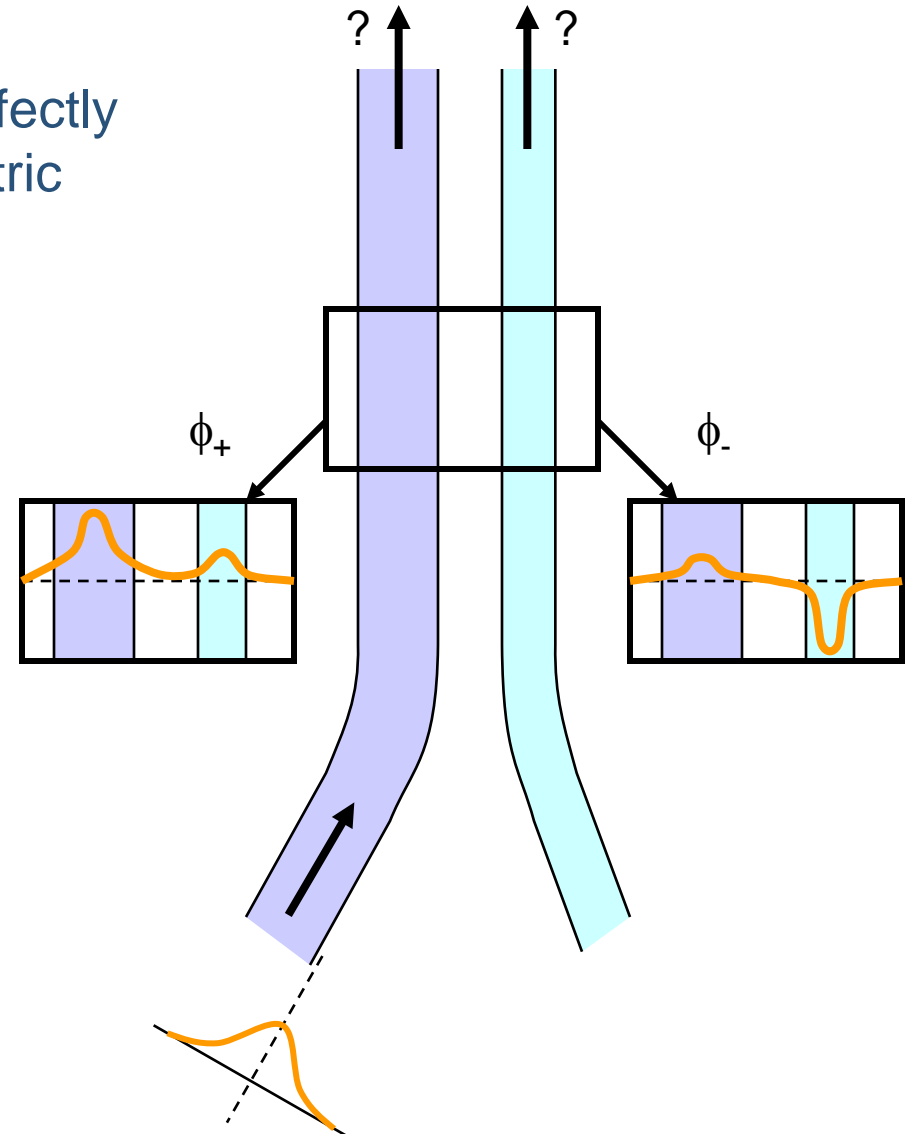
$$\Psi(x, z = L) =$$

$$c_+ e^{-j\beta_+ L} \left(\phi_+ + \frac{c_-}{c_+} \phi_- e^{+j(\beta_+ - \beta_-)L} \right)$$

- coupling length L_c

$$L_c = \frac{\pi}{\beta_+ - \beta_-}$$

- coupling amplitude = $c_-/c_+ < 1$
(\rightarrow no longer full coupling)



- From **coupled mode theory** we find the variation of the amplitude in both waveguides:

$$X_1(z) = e^{-j\beta z} \left[\cos(\delta z) - i \frac{\Delta}{\delta} \sin(\delta z) \right]$$

$$X_2(z) = e^{-j\beta z} \left[-i \frac{\kappa_{21}}{\delta} \sin(\delta z) \right]$$

- With:

$$\beta = (\beta_1 + \beta_2 + \kappa_{11} + \kappa_{22}) / 2 \quad (\beta_{1,2} = \text{modes of single waveguide})$$

$$\kappa = \sqrt{\kappa_{12}\kappa_{21}}$$

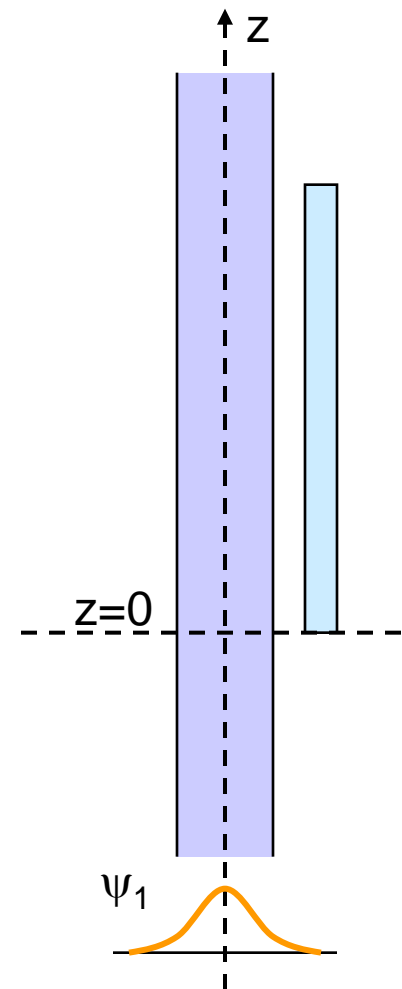
$$\Delta = (\beta_1 - \beta_2 + \kappa_{11} - \kappa_{22}) / 2 \quad (\Delta = \text{Phase mismatch})$$

$$\delta = \sqrt{\Delta^2 + \kappa^2}$$

- And:

$$\kappa_{12} = \frac{k_0^2}{2} \int (n_{12}^2 - n_1^2) \psi_1(x) \psi_2(x) dx$$

$$\kappa_{21} = \frac{k_0^2}{2} \int (n_{12}^2 - n_2^2) \psi_1(x) \psi_2(x) dx$$

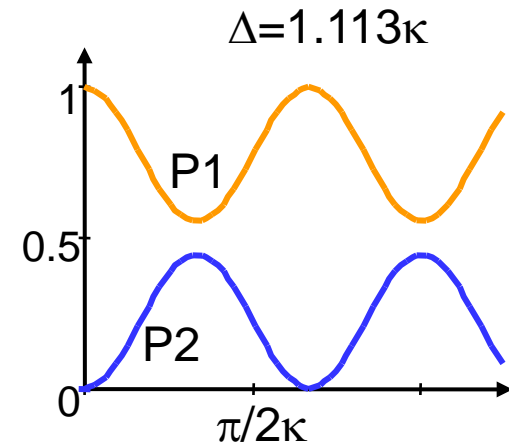
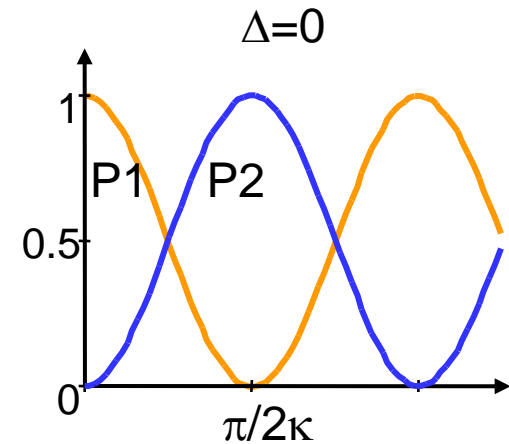


Symmetric waveguide: $\kappa_{12} = \kappa_{21} = \kappa$

From CMT we find:

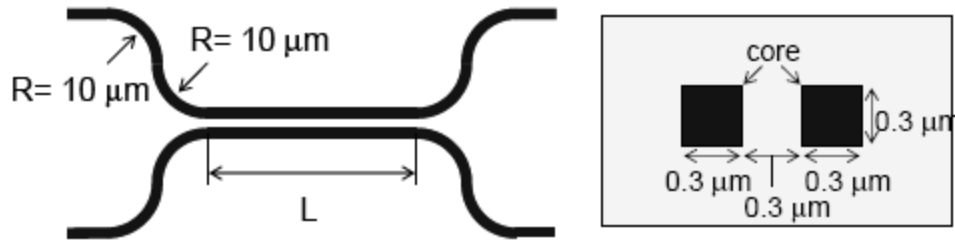
- Periodic power exchange:
 - no phase mismatch ($\Delta = 0$)
 - full coupling
 - = synchronous coupling
 - Increasing phase mismatch ($\Delta < \kappa$)
 - less coupling
 - shorter period
 - = asynchronous coupling
 - Maximal coupled power

$$= \frac{\kappa^2}{\kappa^2 + \Delta^2}$$
 - Large phase mismatch ($\Delta \gg \kappa$)
 - no coupling



H. Yamada e.a., PTL 17, p. 585 (2005)

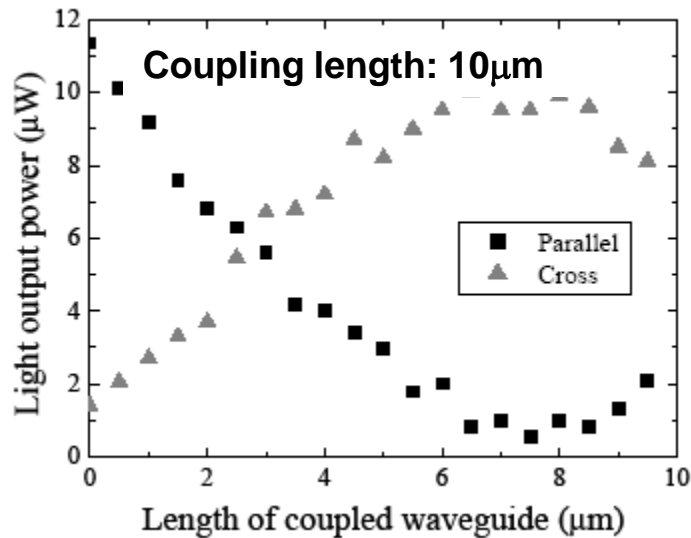
Experimental results



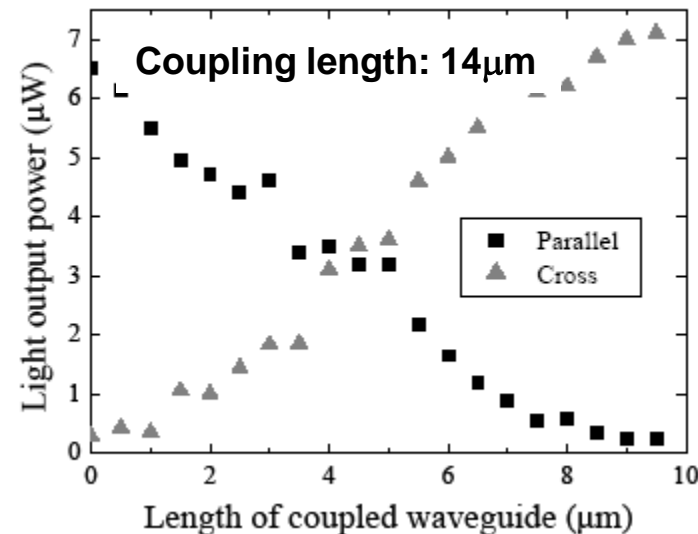
TM mode less confined

→ **stronger overlap**

→ **shorter coupling length !**



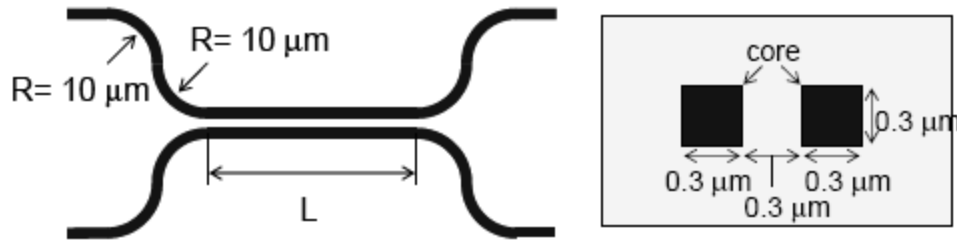
E □ Substrate



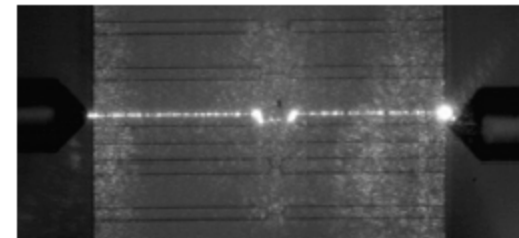
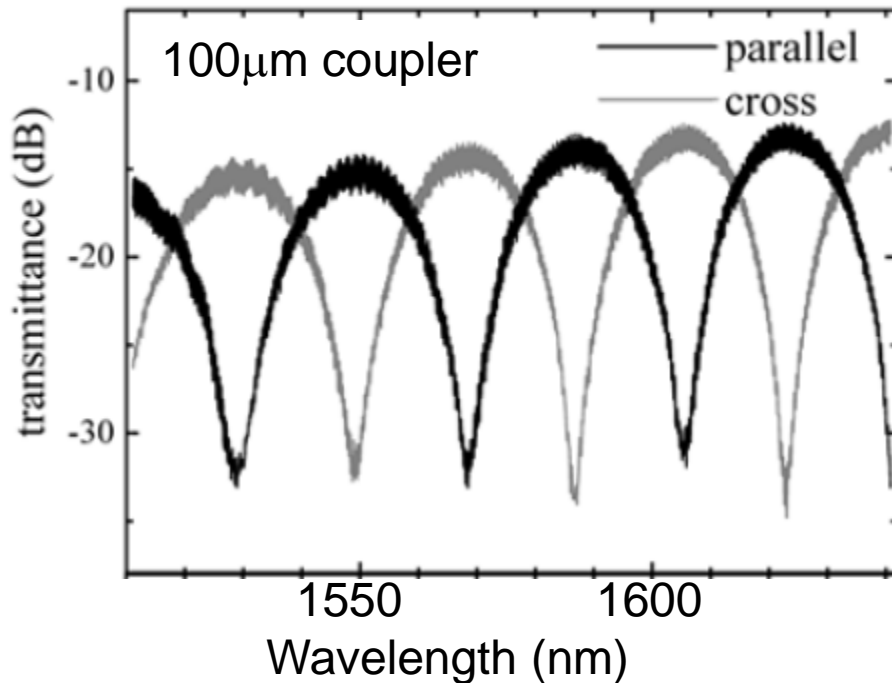
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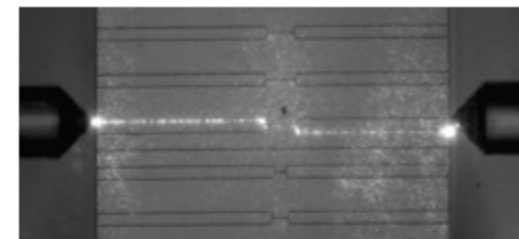
Experimental results



Long couplers or strongly wavelength dependent !



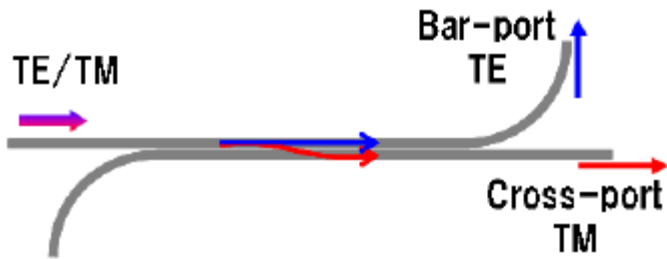
$\lambda = 1534 \text{ nm}$



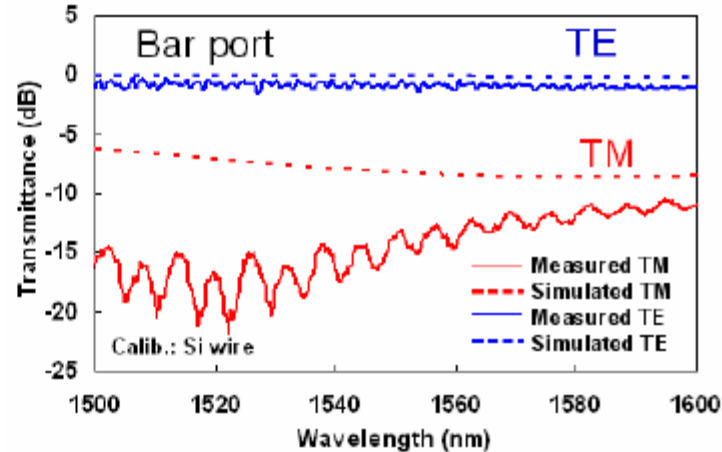
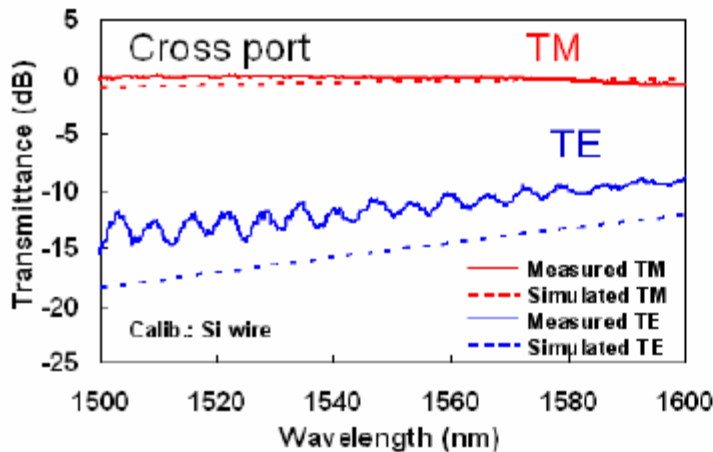
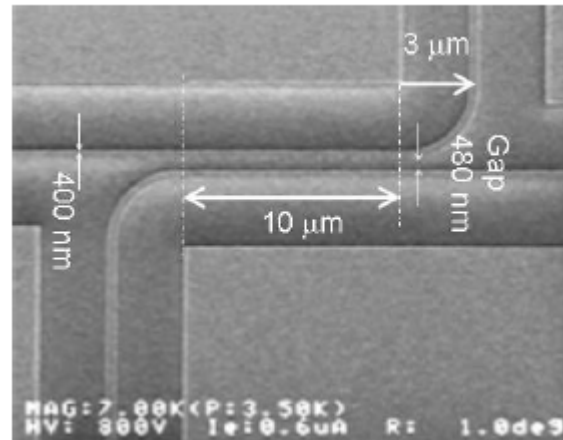
$\lambda = 1563 \text{ nm}$

Fukuda e.a., OE 14(25), p. 12401 (2006)

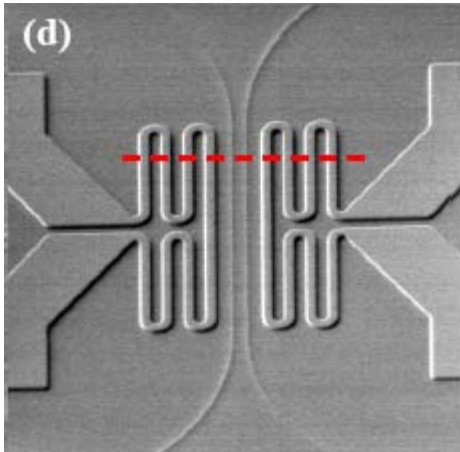
- Use as polarization splitter



Coupling length $TM \ll TE$

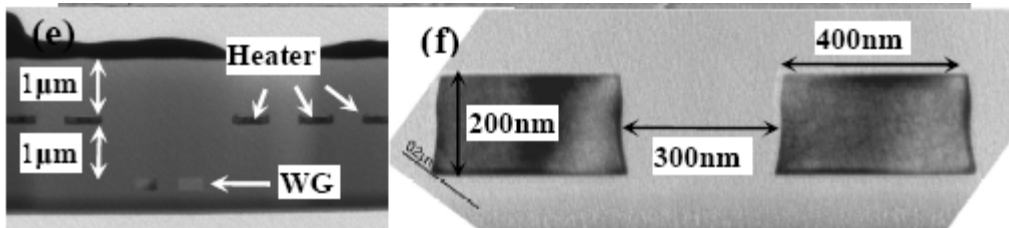


Fine tuning



Heaters can be used to fine tuning the coupling ratio by making coupler asymmetric

Cross-section



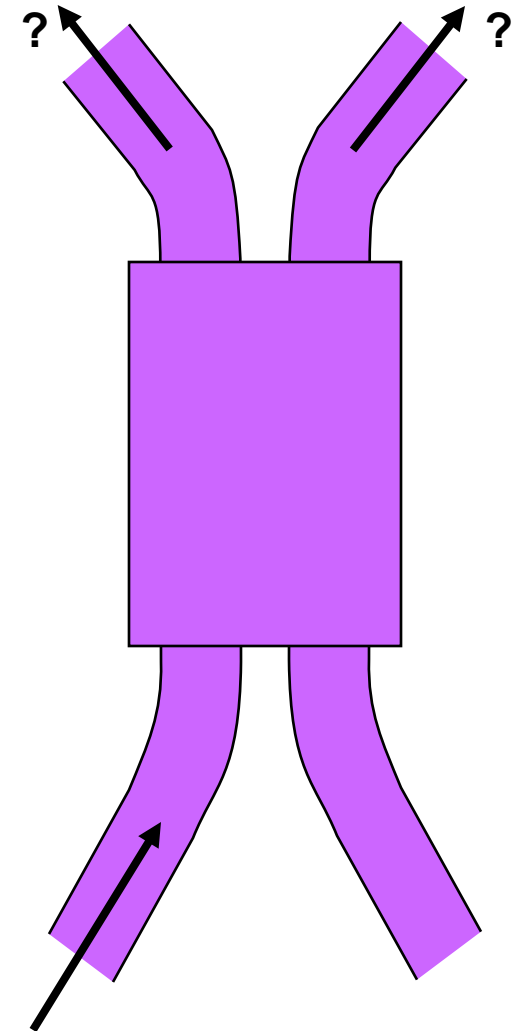
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- Central section = broad waveguide
 - multimodal
 - multiple access waveguides

- Self-Imaging principle:

In multimodal waveguides an input field will be periodically reproduced in a single or multiple image.

 - 1 x N couplers possible
 - Cross-couplers possible
 - Arbitrary splitting ratios



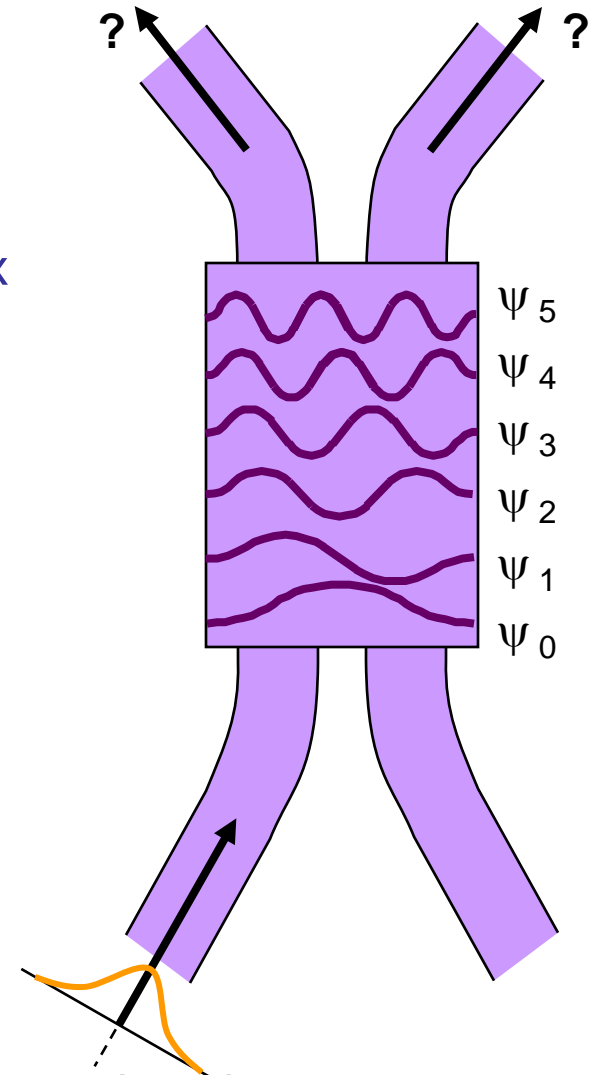
- Decompose incident field in eigenmodes of the MMI:

$$\Psi(x,0) = \sum_{i=0}^{N-1} c_i \psi_i(x) \quad \text{with} \quad c_i = \int \Psi(x,0) \psi_i(x) dx$$

(ignore radiative modes if $\Psi(x,0)$ sufficiently narrow compared to the MMI)

- After propagation over distance z :

$$\begin{aligned} \Psi(x,z) &= \sum_{i=0}^{N-1} c_i \psi_i(x) e^{-j\beta_i z} \\ &= e^{-j\beta_0 z} \sum_{i=0}^{N-1} c_i \psi_i(x) e^{j(\beta_0 - \beta_i) z} \end{aligned}$$



- Approximate MMI modes by the modes for an infinite refractive index contrast:

$$\psi_i(x) = \cos(k_{x,i}x) \quad \text{for } i \text{ even}$$

$$\psi_i(x) = \sin(k_{x,i}x) \quad \text{for } i \text{ odd}$$

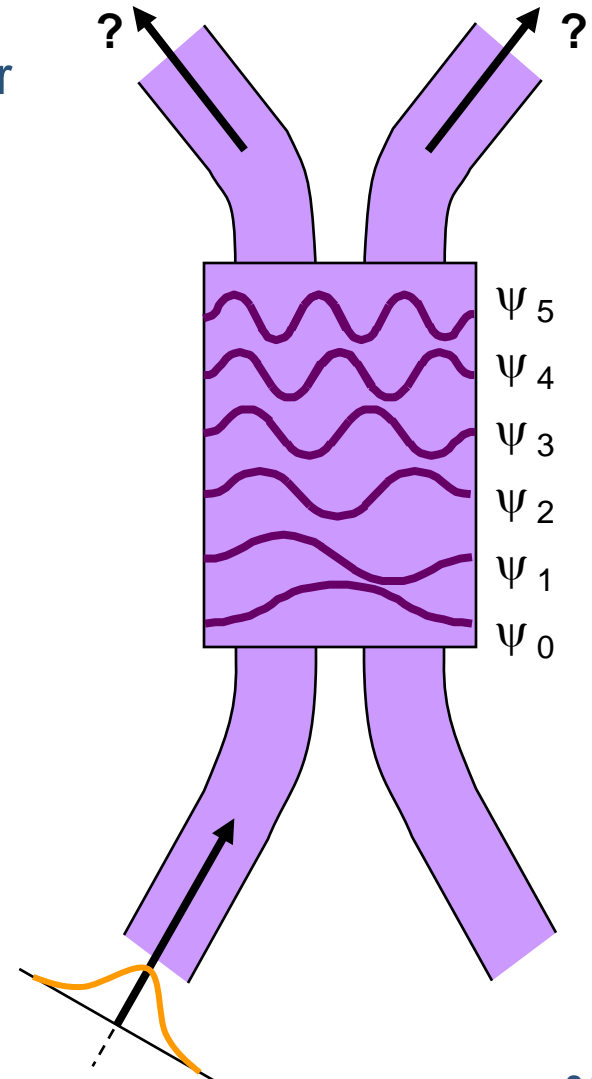
$$\text{with } k_{x,i} = \frac{(i+1)\pi}{W}$$

(good for high contrast waveguides)

- Propagation constant β_i

$$k_{x,i}^2 + \beta_i^2 = k_0^2 n_r^2$$

$$\text{therefore } \beta_i \approx k_0 n_r - \frac{(i+1)^2 \pi \lambda_0}{4 n_r W^2}$$



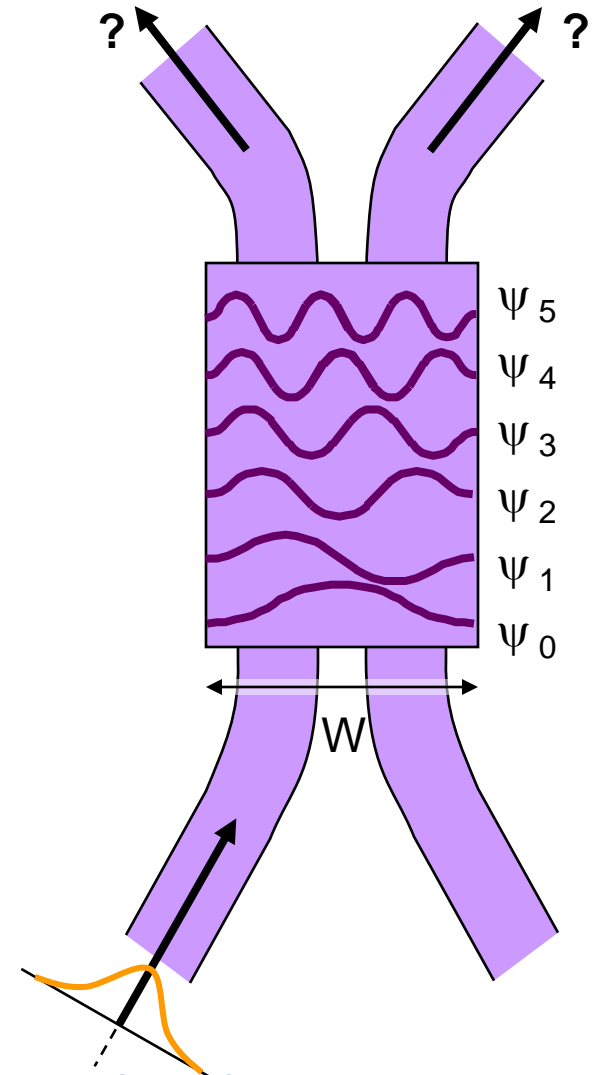
- Difference in propagation constants:

$$(\beta_0 - \beta_i) = i(i+2) \frac{\pi \lambda_0}{4n_r W^2} = \frac{i(i+2)\pi}{3L_\pi}$$

$$\text{with } L_\pi = \frac{\pi}{\beta_0 - \beta_1} = \frac{4n_r W^2}{3\lambda_0}$$

- The Ψ after propagation length L

$$\Psi(x, L) = \sum_{i=0}^{N-1} c_i \psi_i(x) e^{j \frac{i(i+2)\pi}{3L_\pi} L}$$



- The field Ψ in $z=L$

$$\Psi(x, L) = \sum_{i=0}^{N-1} c_i \psi_i(x) e^{j \frac{i(i+2)\pi L}{3L_\pi}}$$

- For $L = 6L_\pi$

$$\Psi(x, 6L_\pi) = \Psi(x, 0)$$

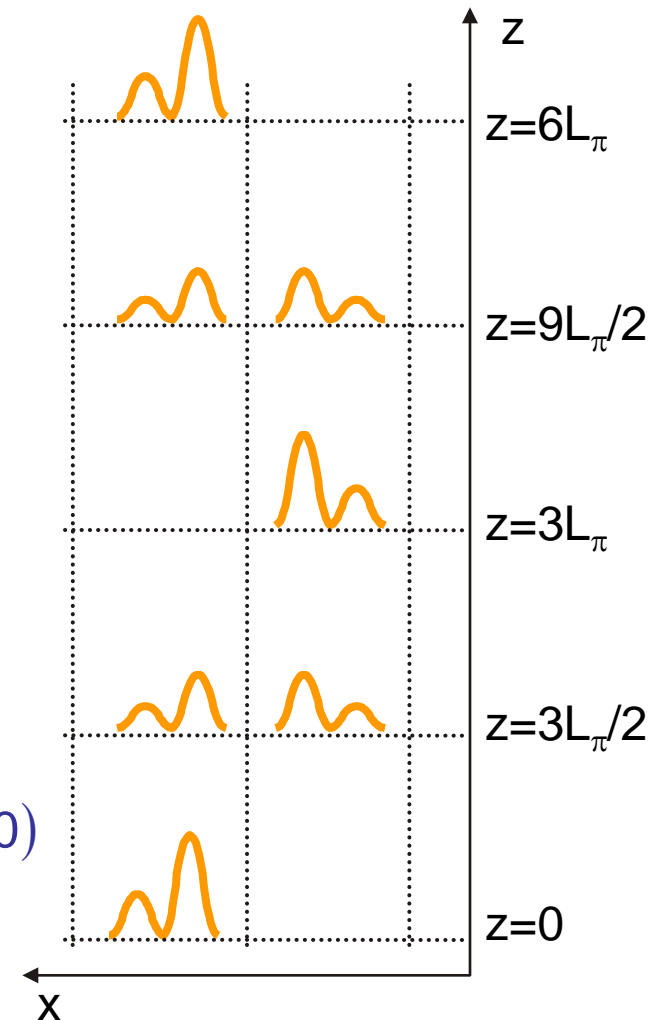
- For $L = 3L_\pi$

$$\Psi(x, 3L_\pi) = \Psi(-x, 0)$$

- For $L = 3p/2 L_\pi$ with p odd

$$\Psi\left(x, \frac{p}{2} 3L_\pi\right) = \frac{1 + (-j)^p}{2} \Psi(x, 0) + \frac{1 - (-j)^p}{2} \Psi(-x, 0)$$

→ two images (3dB coupling)

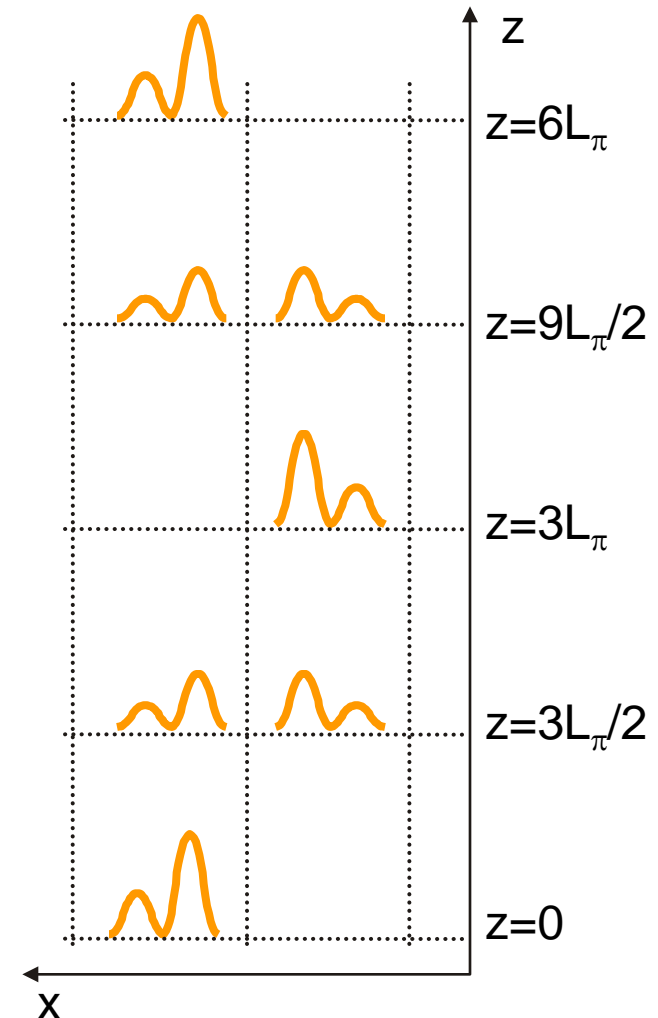


- The field Ψ in $z=L$

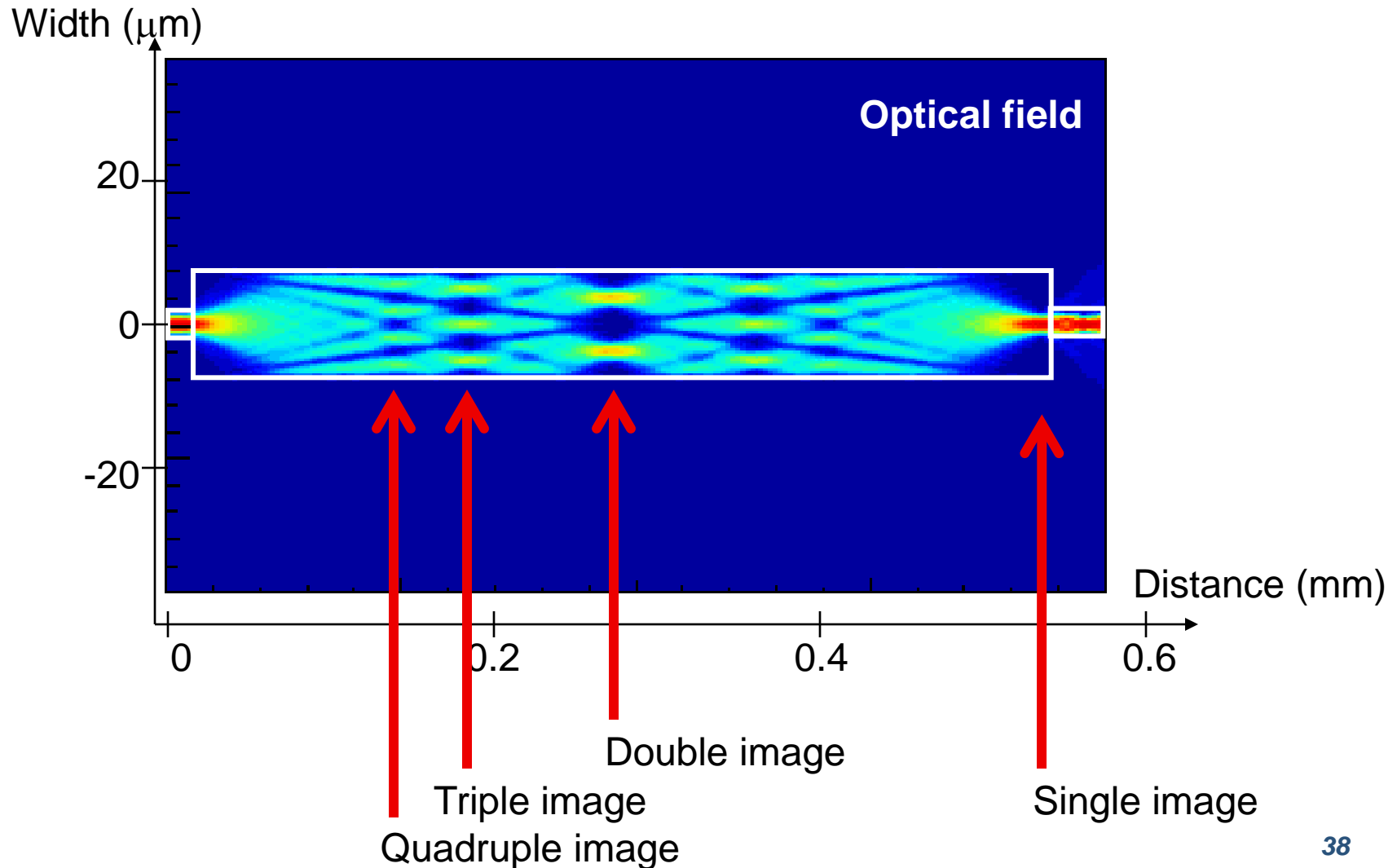
$$\Psi(x, L) = \sum_{i=0}^{N-1} c_i \psi_i(x) e^{j \frac{i(i+2)\pi L}{3L_\pi}}$$

- Multiple images:
N-fold image at distance $L = 3p/N L_\pi$
with p and N whole numbers without
common divisors

→ amplitude = $1/\sqrt{N}$



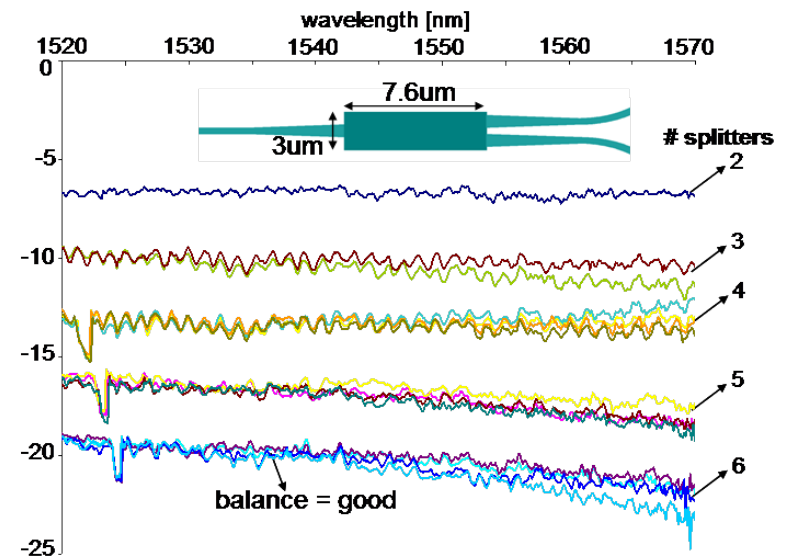
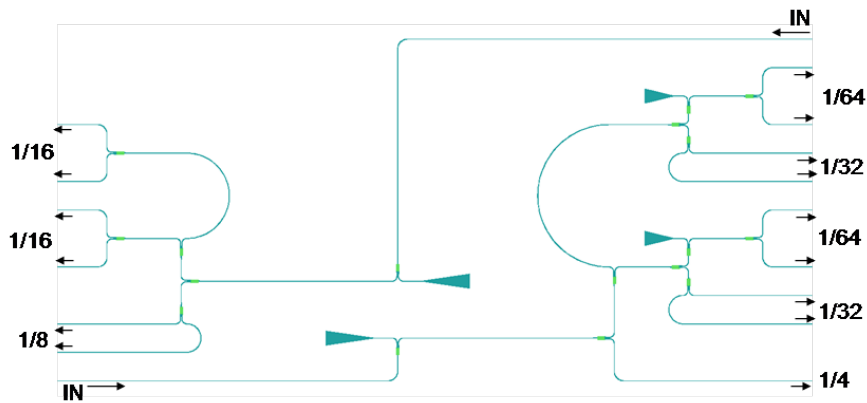
- BPM simulation of an MMI (15 x 520 μm)



- Other
 - Variable coupling ratio possible but more complex design
 - (Anti-)Symmetric excitation allows for shorter couplers
 - In real devices: replace W by W_{eff}

- Experimental results
 - Standard coupler ($3\mu\text{m} \times 7.6\mu\text{m}$)

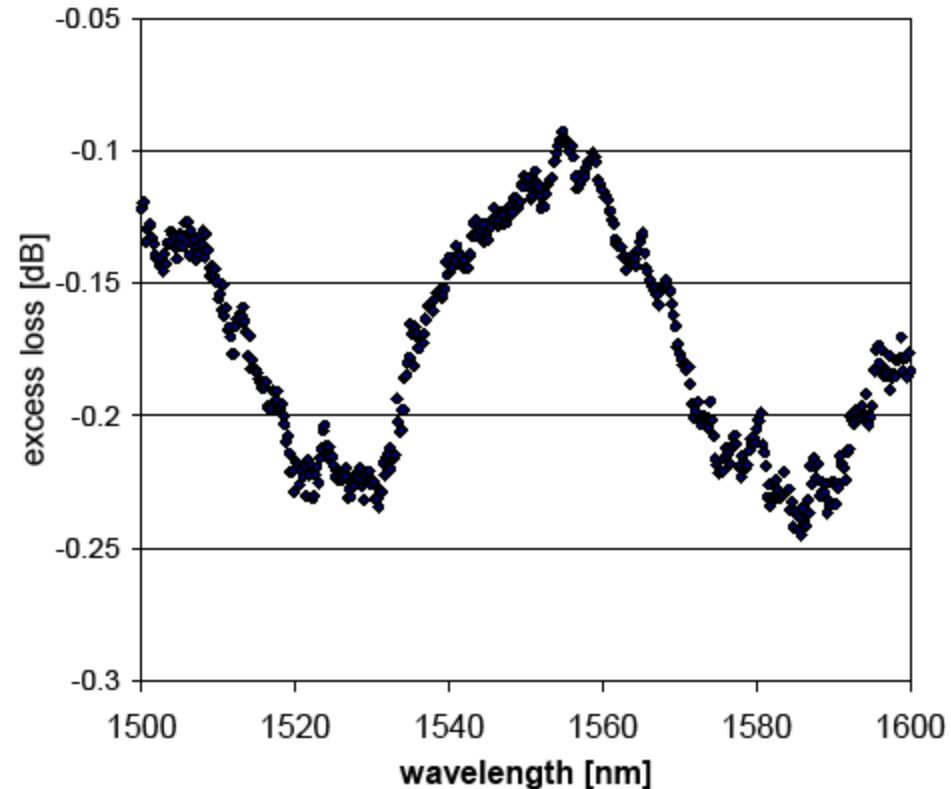
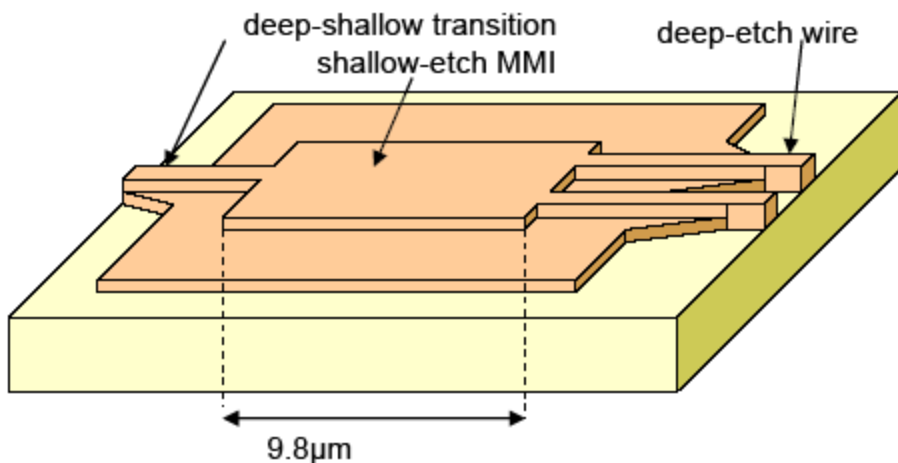
(<0.3dB excess loss)



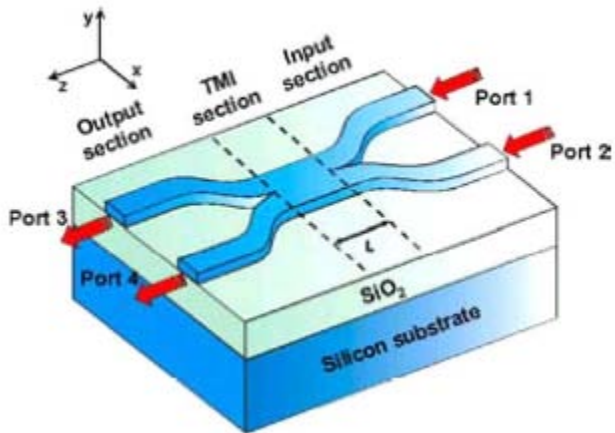
Experimental results

- Shallowly etched coupler ($3\mu\text{m} \times 7.6\mu\text{m}$)

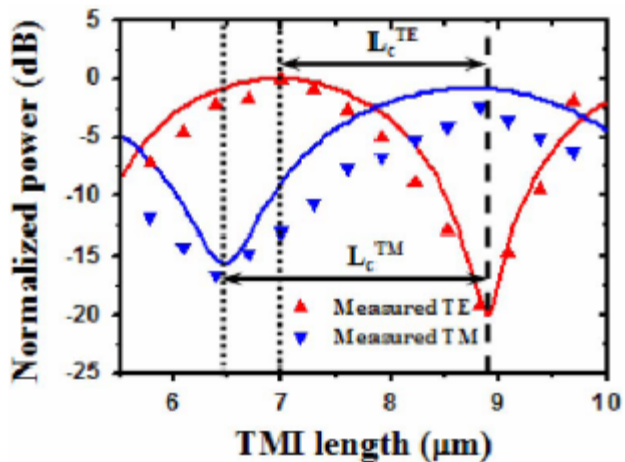
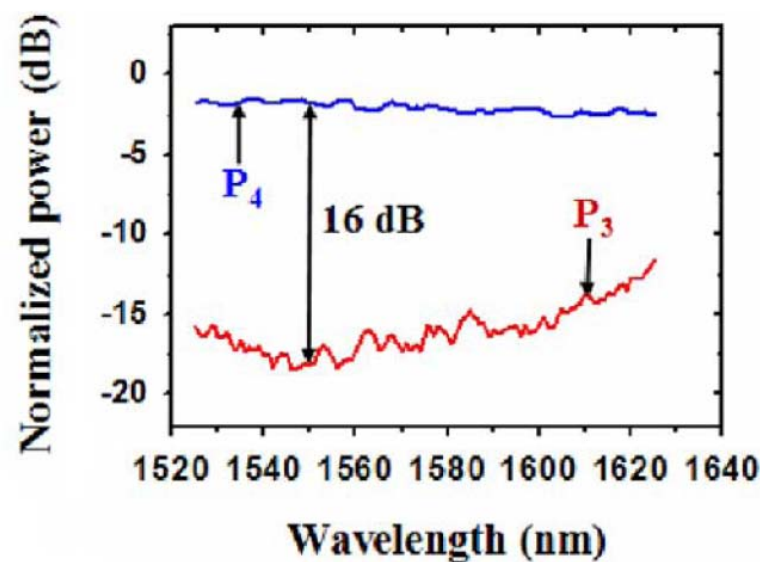
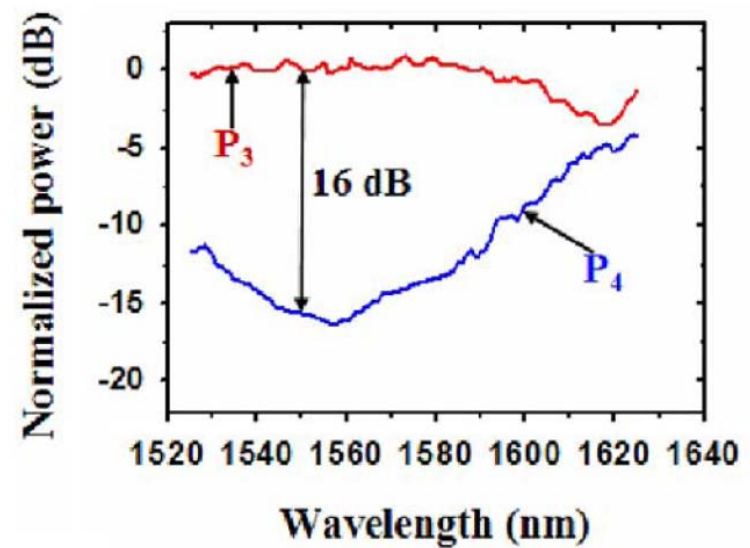
(<0.2dB excess loss)



- Use as polarization splitter
 - Two mode interference (TMI)

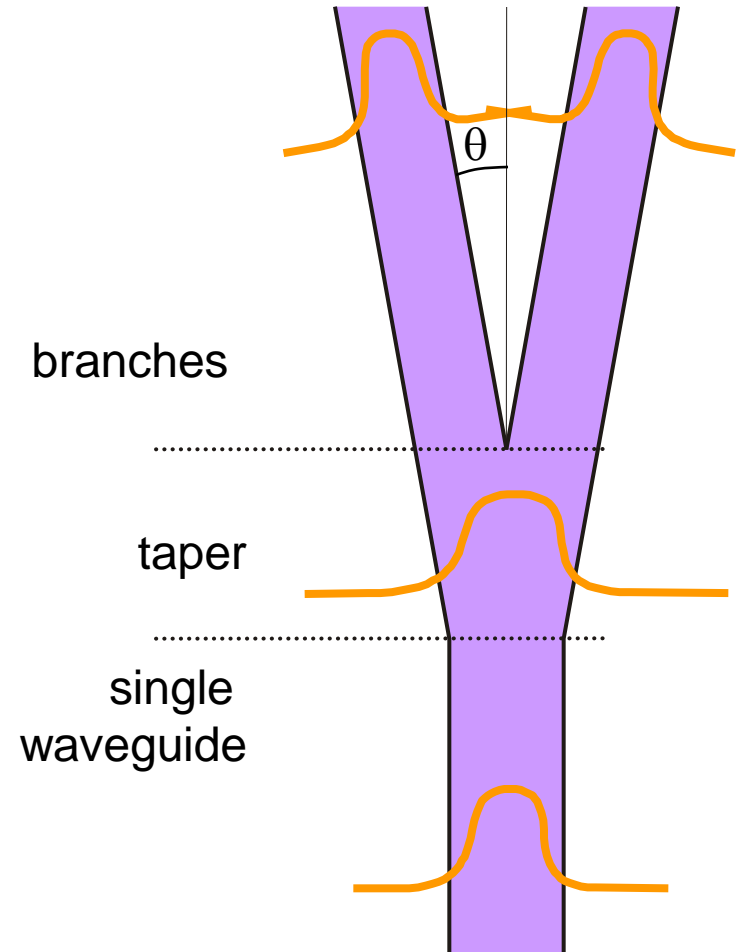


B-K Yang e.a. , PTL 21 (7), p 432 (2010)



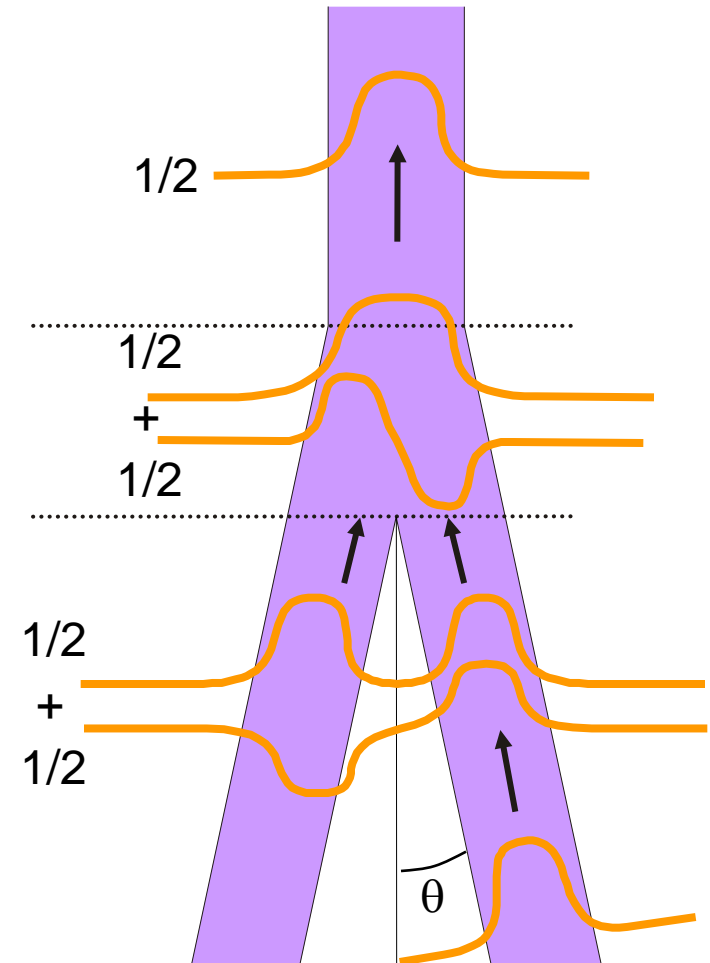
- Outline
 - The Straight Waveguide
 - The Waveguide Bend
 - The Directional Coupler
 - Star coupler
 - The Multimode Interference Coupler
 - **The Y-junction**
 - The Mach–Zehnder Interferometer
 - The AWG

- **Y-junction =**
 straight waveguide
 +
 taper
 +
 two branches
- Aperture angle θ :
 should be sufficiently small
- Then: no splitting loss
 = adiabatic Y-junction



- Reversed junction:
a mode in only 1 branch
- Decompose into local supermodes
 - symmetric supermode is squeezed into the ground mode
 - Anti-symmetric supermode is squeezed into the first-order mode
→ first-order mode is not guided in a single-mode waveguide

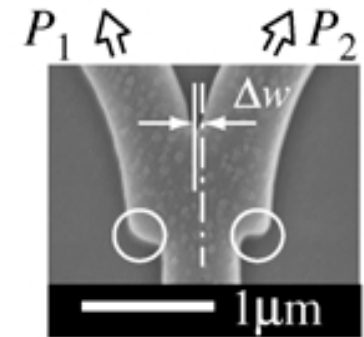
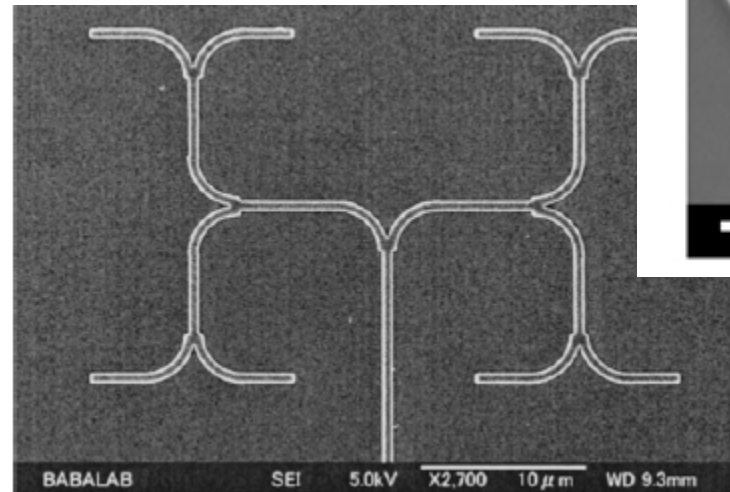
→ **half of the power is lost !!!**



(a)		2.0 dB
(b)		0.5 dB
(c)		0.5 dB
(d)		< 0.1 dB
(e)		0.3 dB
(f)		< 0.1 dB

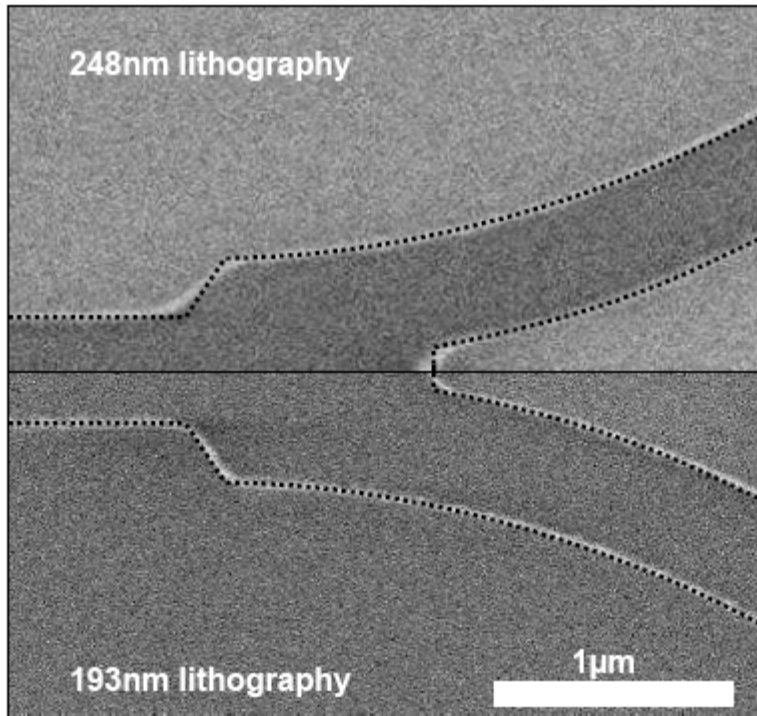
Large **losses** for standard Y-junction
Need **improved** design !!!

Example



- Simulation: < 0.1 dB excess loss
- Experiment: 0.3 dB excess loss
- Some imbalance due to opt. Prox.

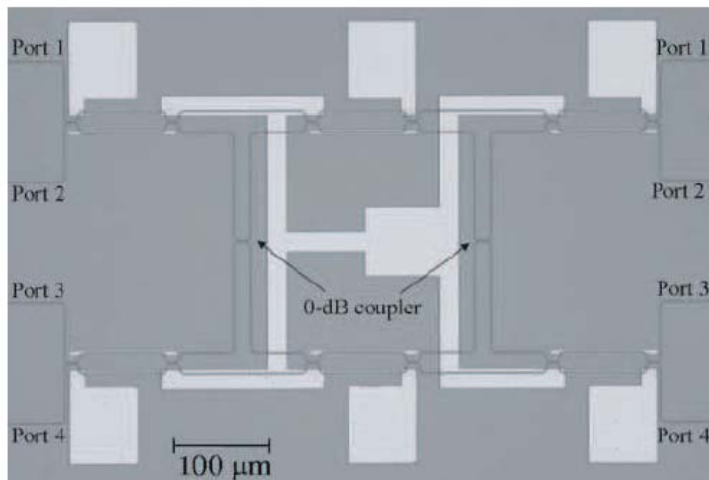
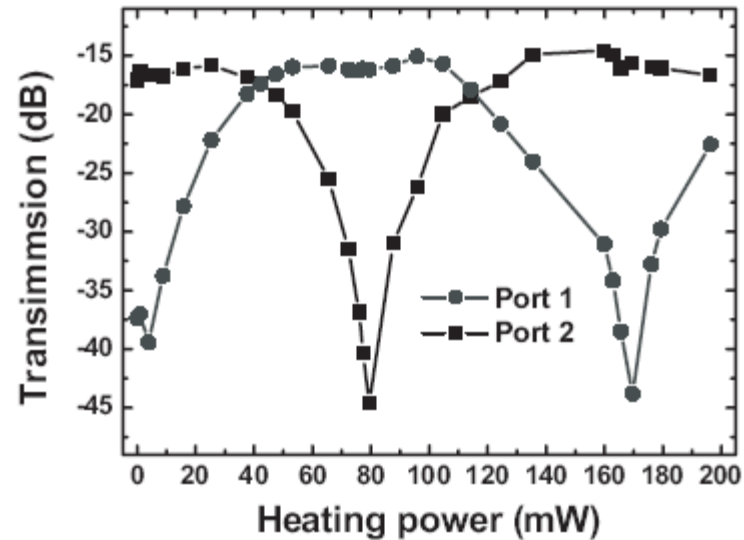
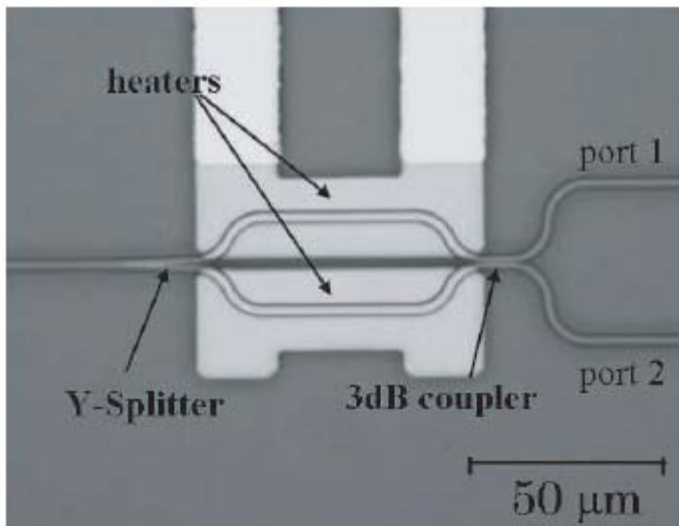
- Need very high lithographic resolution



Picture: Bogaerts e.a. JSTQE, 2010

Theory: Fukazawa e.a. Jpn JAP 41, p L1461 (2002)

- Use Y-junctions to fabricate TO-switches



4 x 4 switch

Yamada e.a., PIERS proc., Beijing, p. 22 (2009)

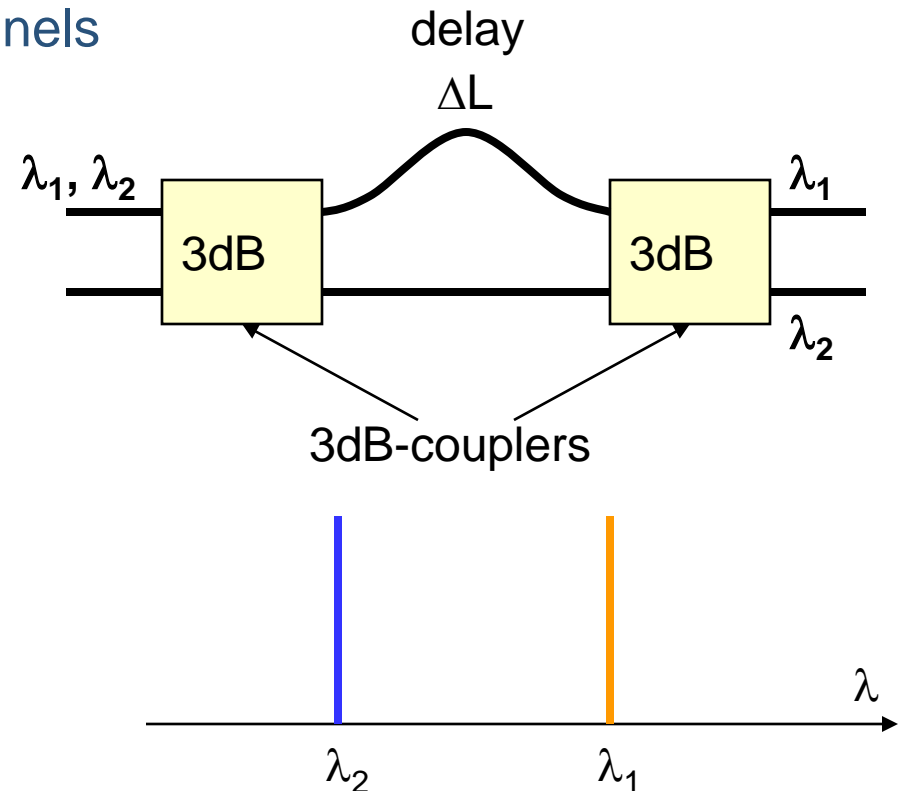
- Outline
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 - **The Mach–Zehnder Interferometer**
 - The AWG

- Mach-Zehnder interferometer:

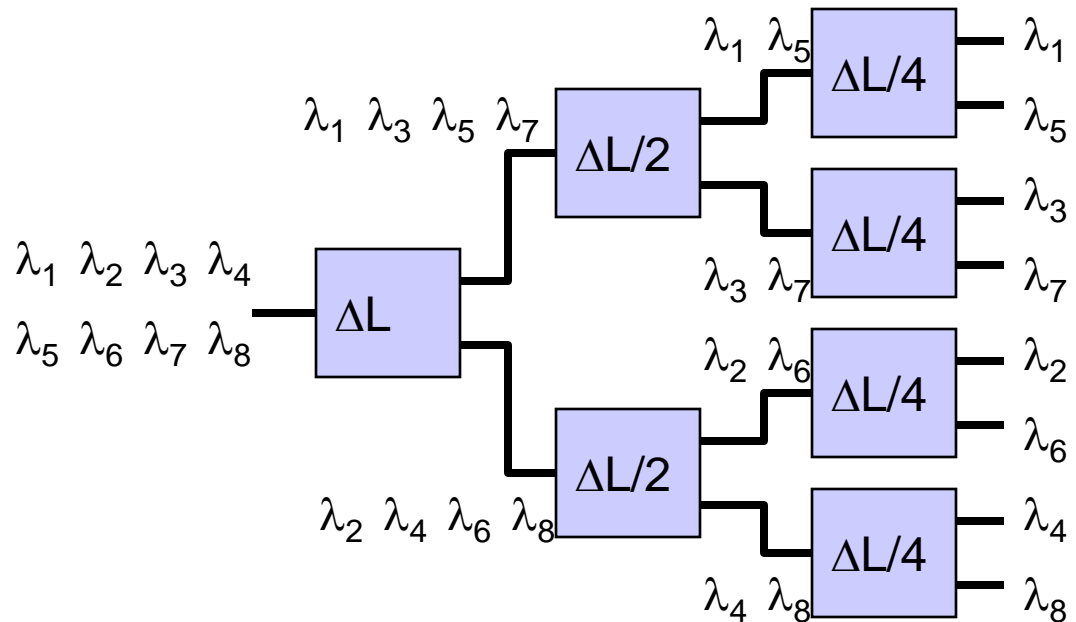
→ Splitting of two wavelength channels when

$$\frac{\lambda_1 - \lambda_2}{\lambda_c} = \frac{\lambda_c}{2n\Delta L}$$

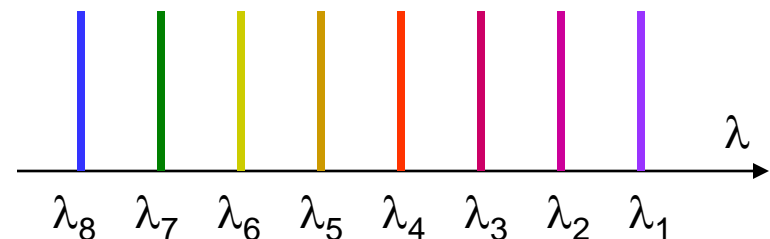
with $\lambda_c = \frac{1}{2}(\lambda_1 + \lambda_2)$



- MZI demultiplexer = cascade of MZI's with smaller delay lengths

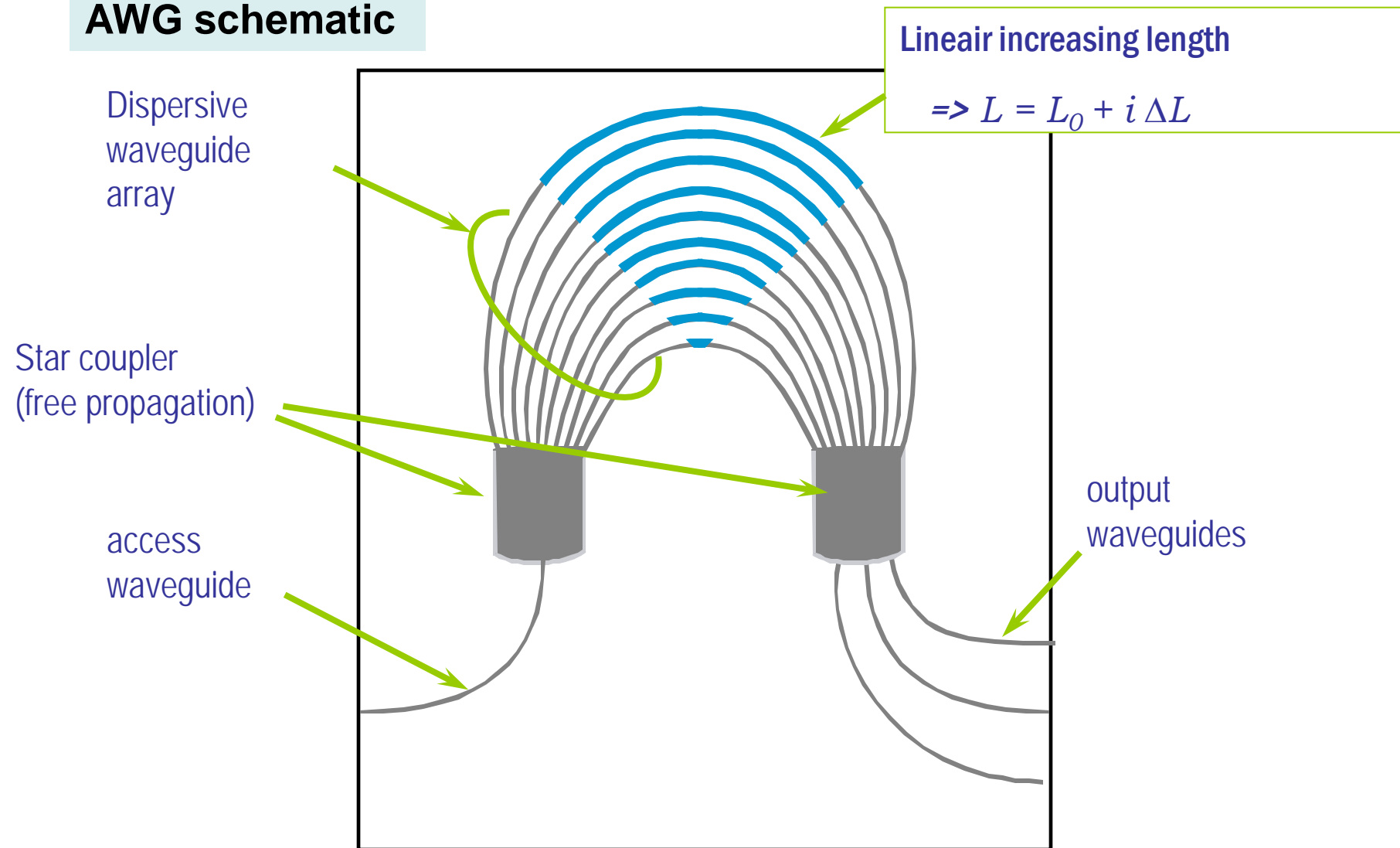


- Very high resolution
- Strict fabrication tolerances

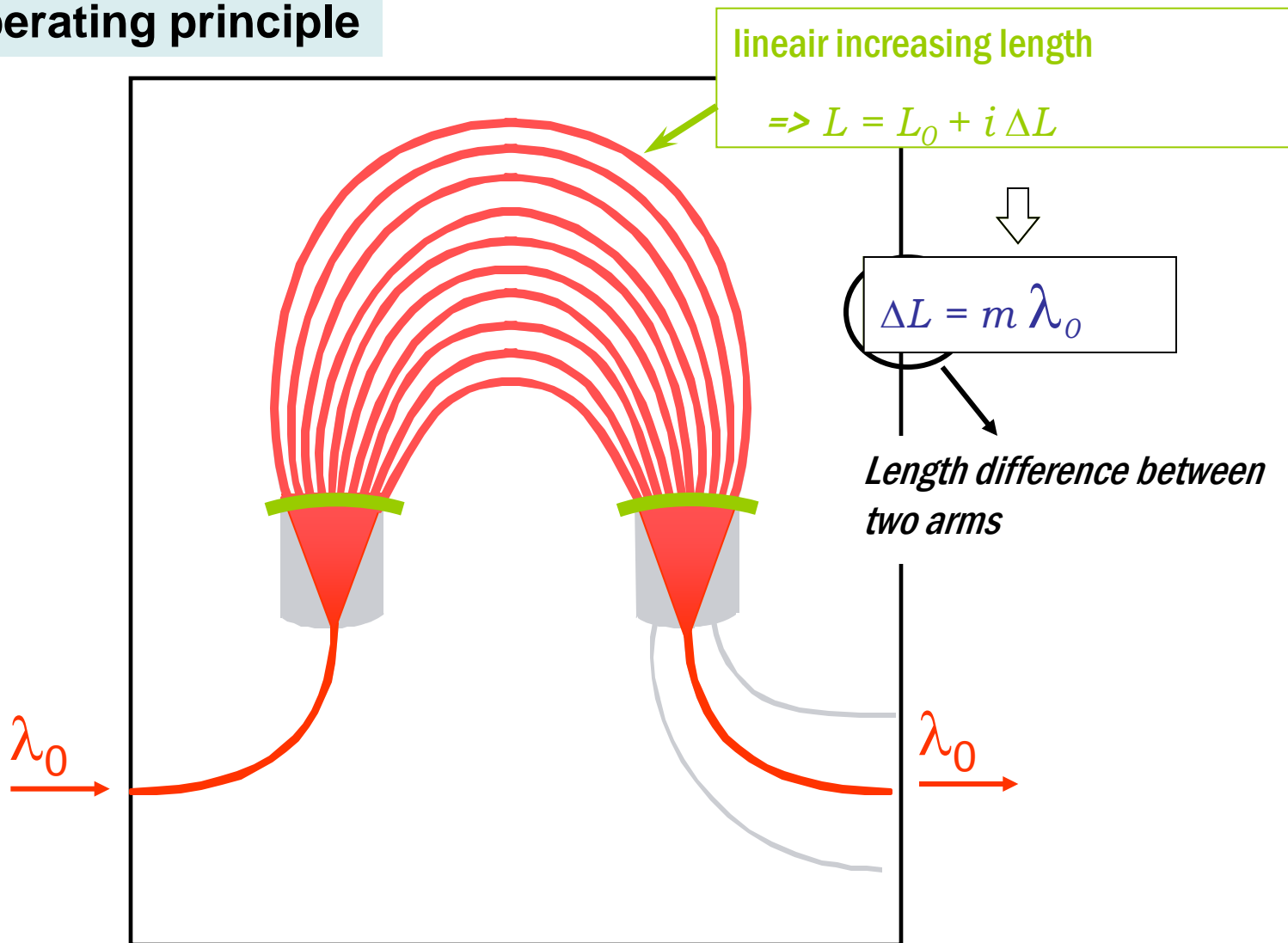


- Outline
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 - **The AWG**

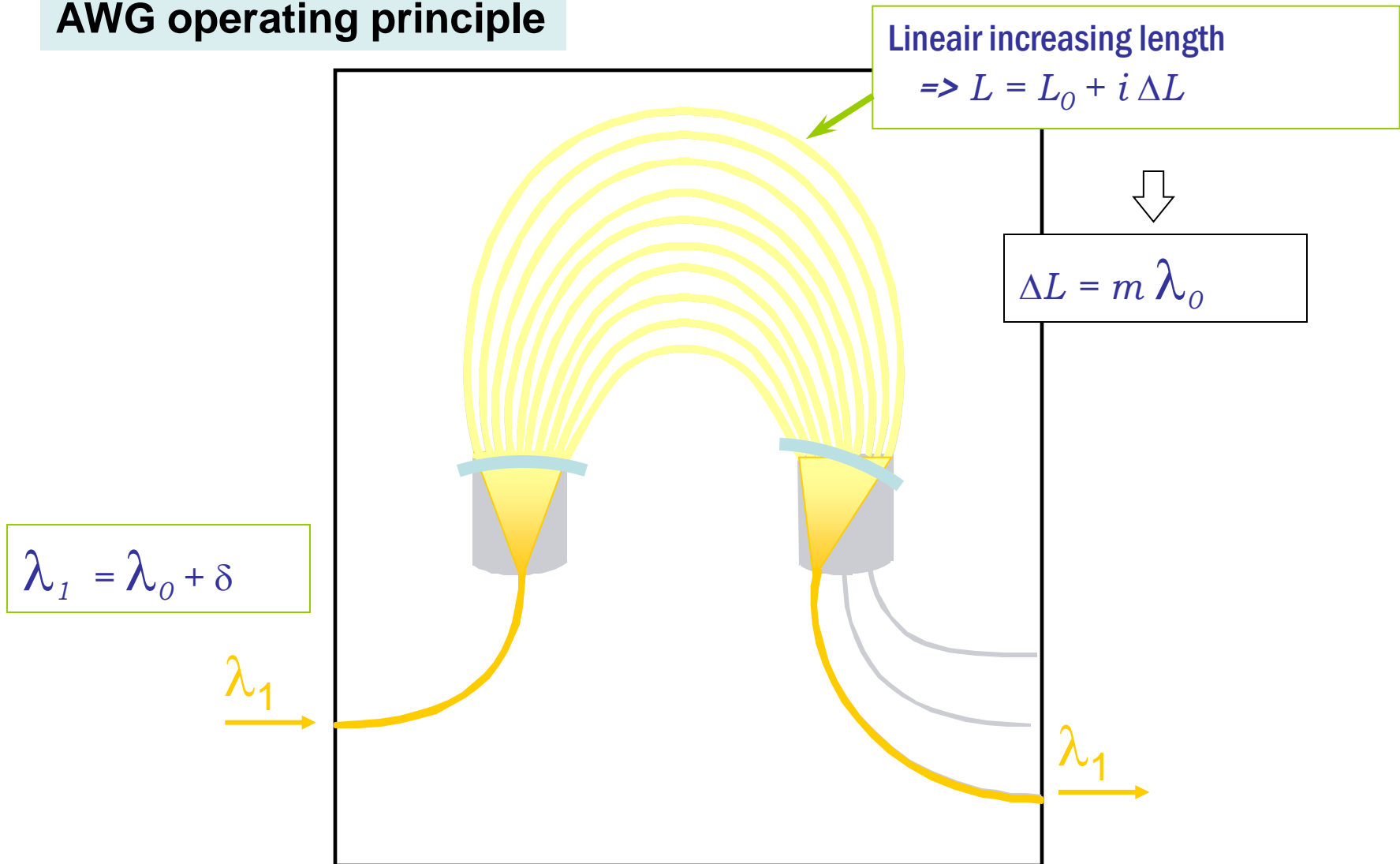
AWG schematic

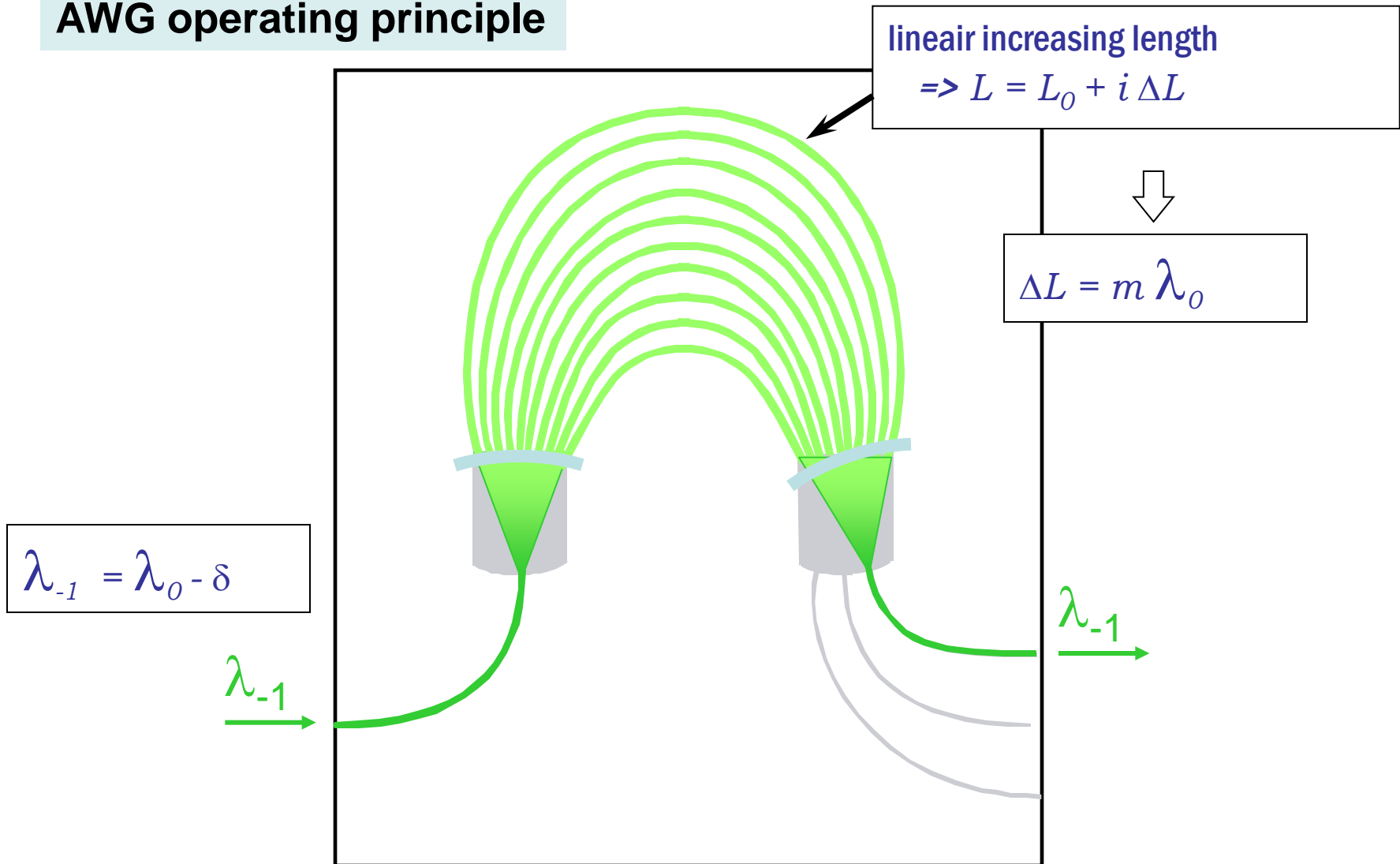


AWG operating principle



AWG operating principle



AWG operating principle


AWG operating principle

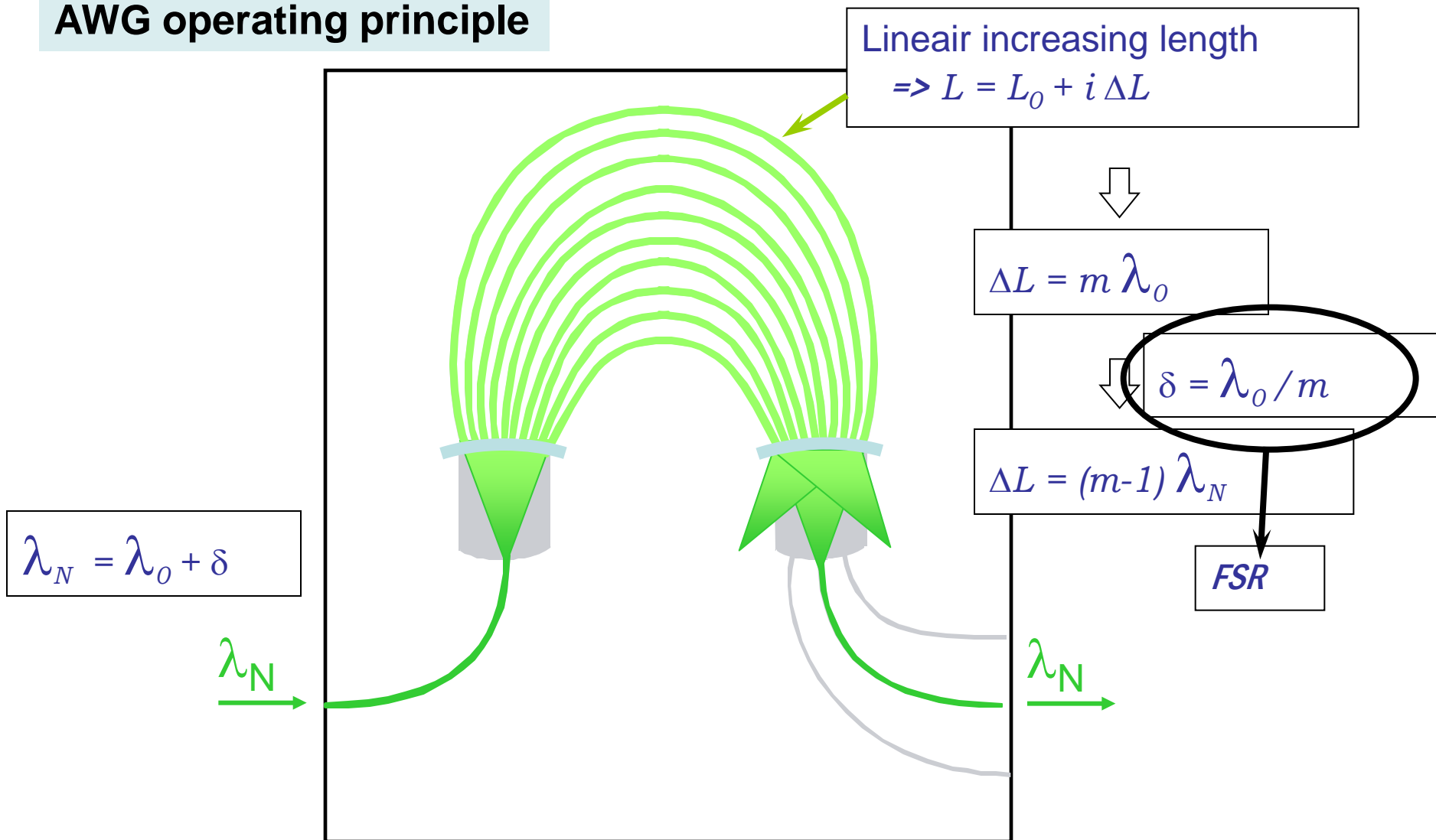
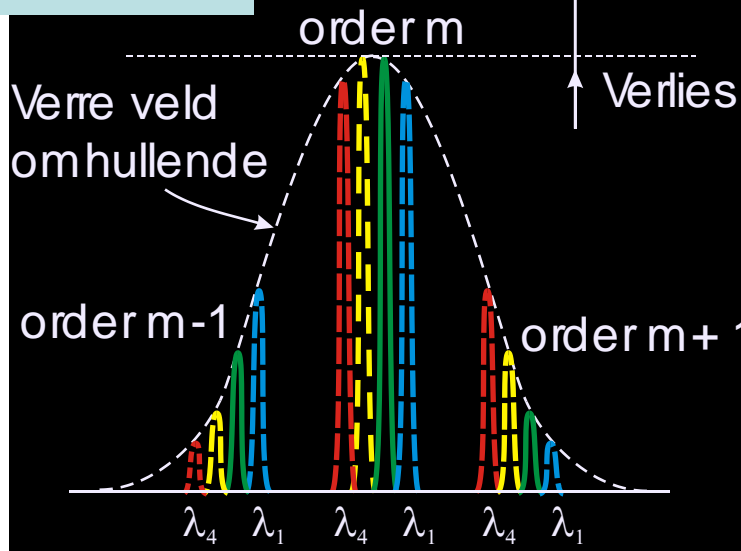
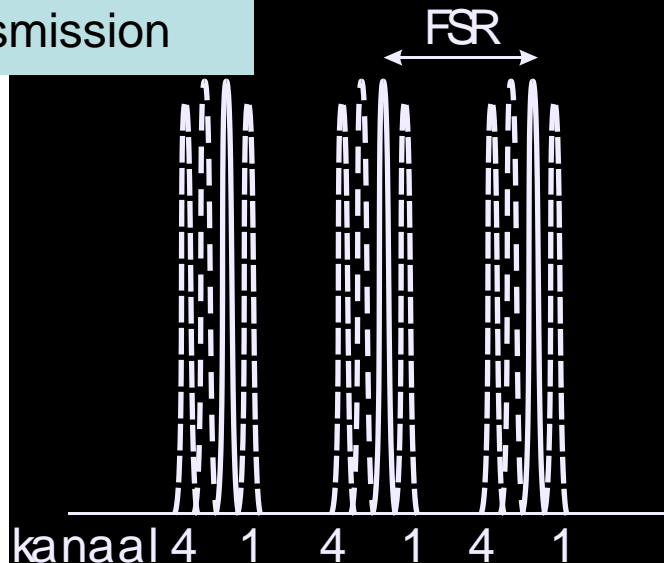


Image plane

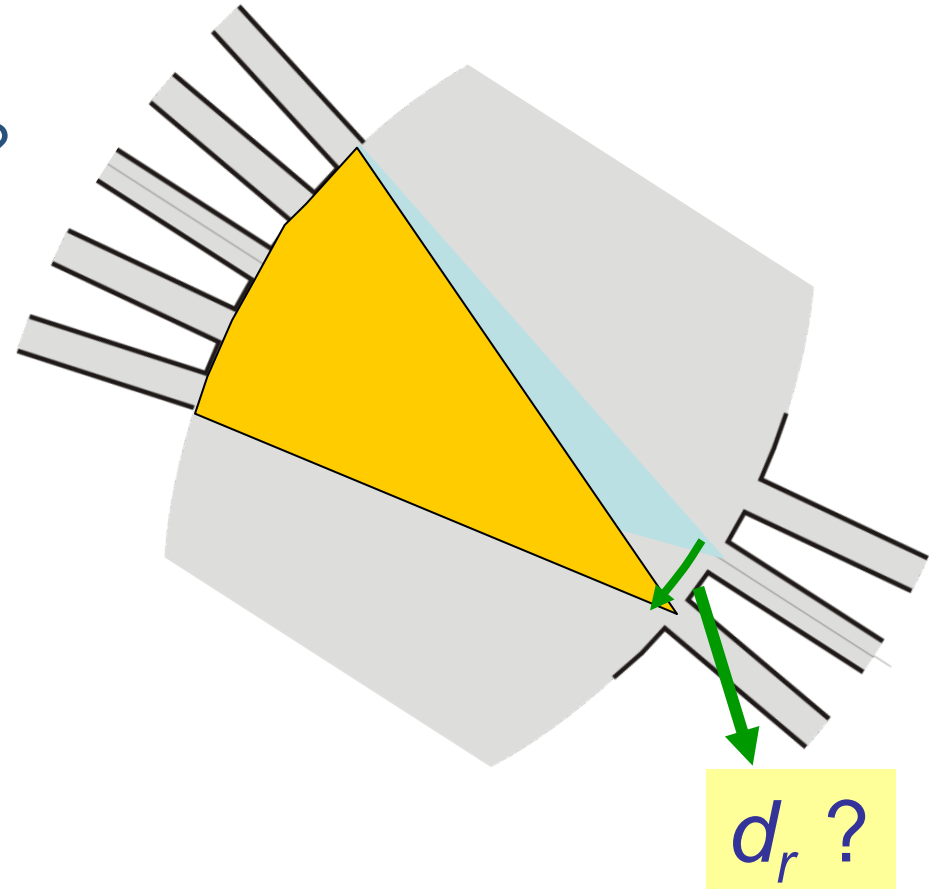


- AWG is characterised by:
 - Periodicity $\Delta\lambda_{\text{FSR}}$
 - Channel spacing $\Delta\lambda_{\text{ch}}$
 - Bandwidth
 - Loss
 - Crosstalk

Transmission



- What is displacement in focal plane for given $\Delta\nu$?

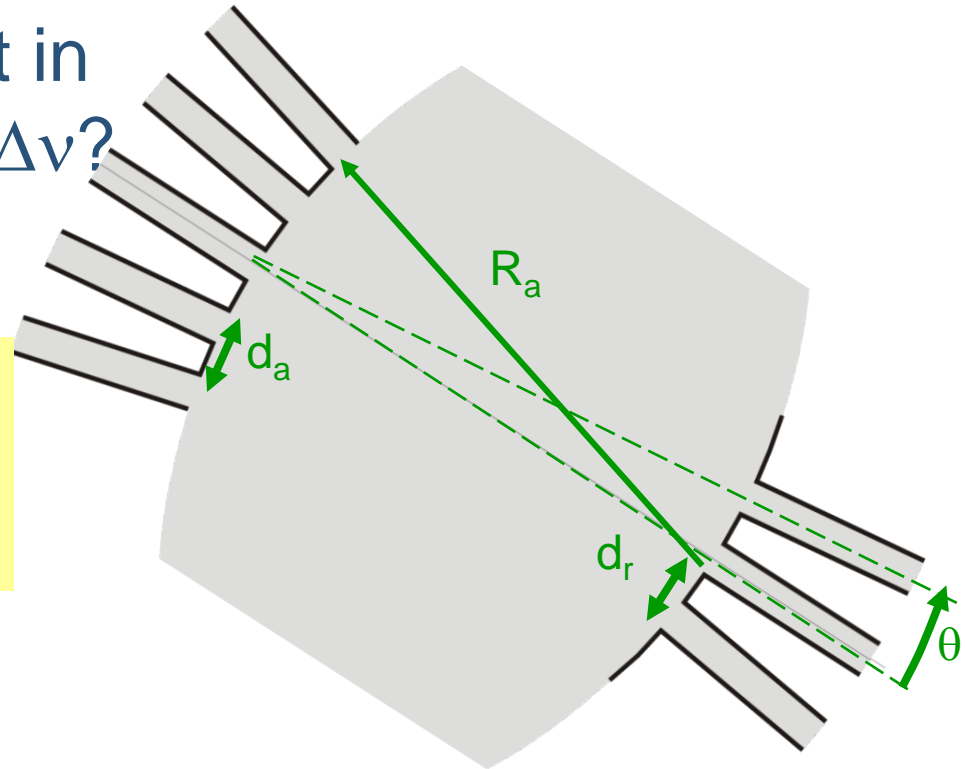


- What is displacement in focal plane for given Δv ?

Determined by
dispersion:

$$D = \frac{ds}{dv}$$

$$\frac{ds}{dv} = R_a \frac{d\theta}{dv}$$



What is d_r for given Δv ?

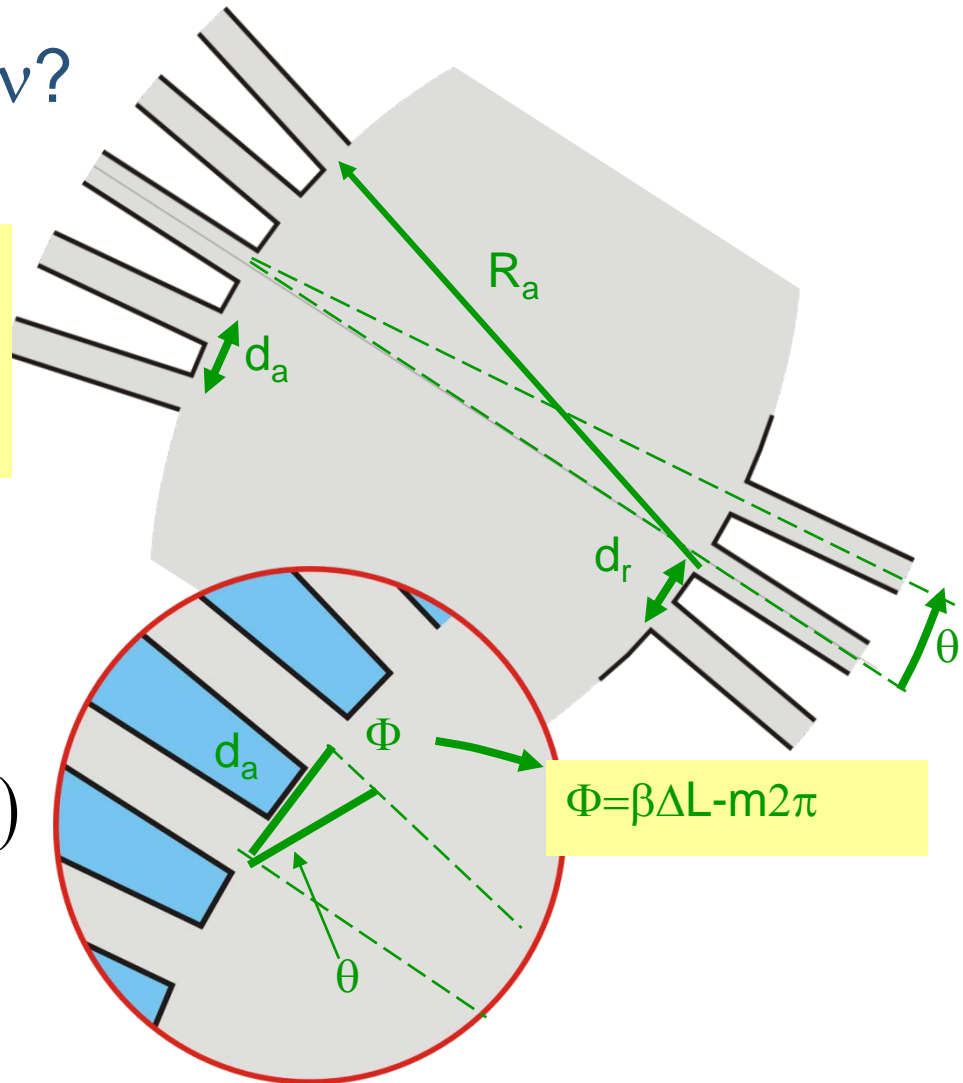
Determined by dispersion:

$$D = \frac{ds}{dv}$$

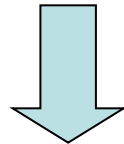
$$\frac{ds}{dv} = R_a \frac{d\theta}{dv}$$

$$d\theta = \frac{\lambda}{2\pi} d\Phi = \frac{\lambda_0}{2\pi n_s} d(\beta\Delta L - 2m\pi)$$

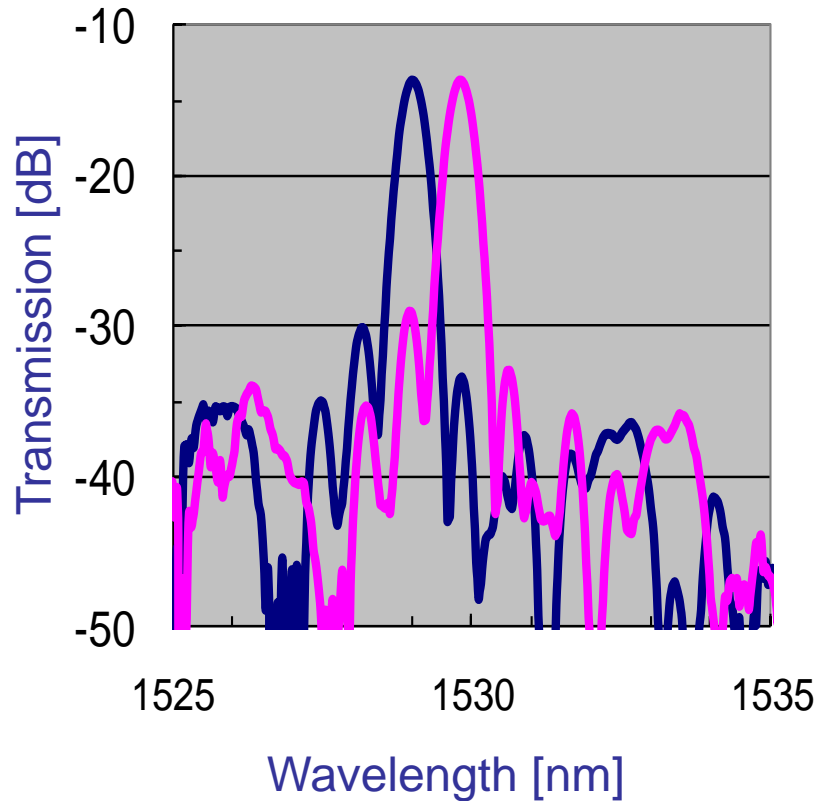
$$\frac{ds}{dv} = R_a \frac{\Delta L}{v_c d_a}$$



- Design parameters
 - channel spacing, bandwidth FSR
- Practical boundary conditions
 - waveguide dimensions, minimum waveguide spacing...



- From this: determine ΔL , dispersion, focal length



Loss

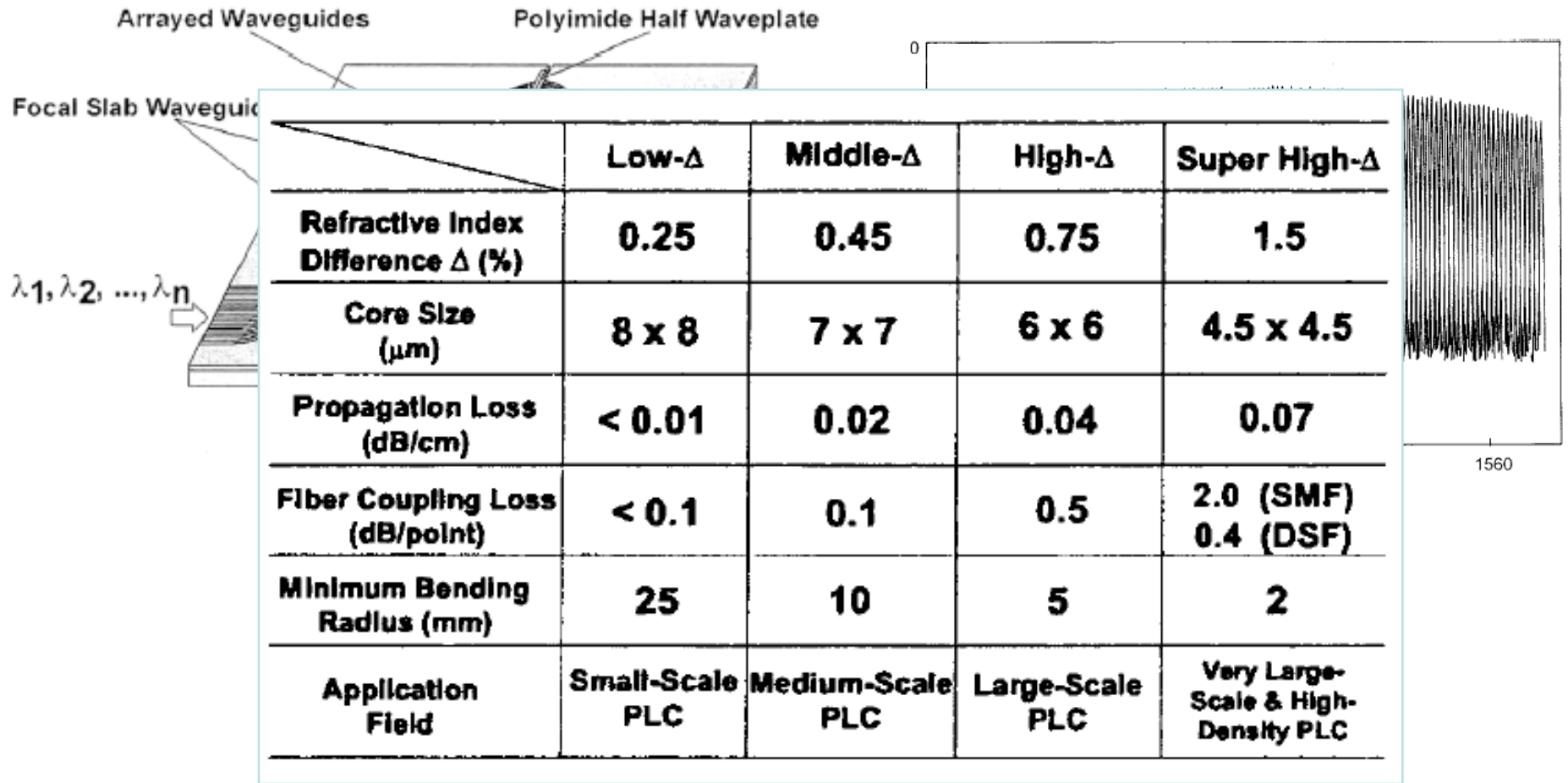
- Waveguide losses
- Imperfect star coupler
- Finite aperture



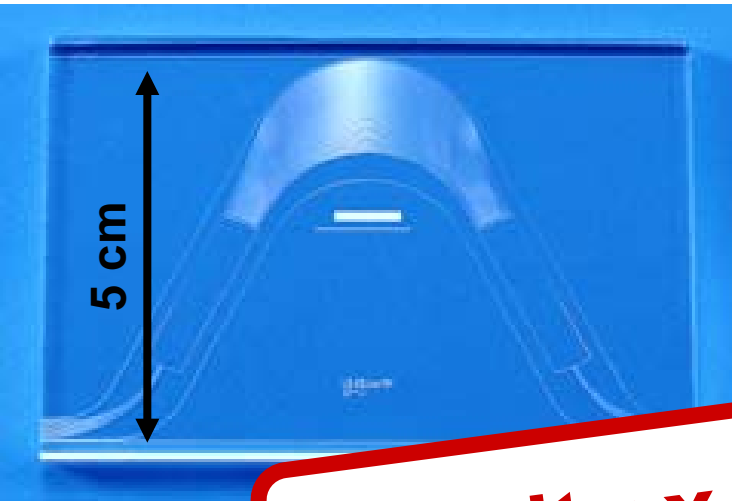
Crosstalk

- Finite aperture
- Overlapping fields in access waveguides
- Phase noise on length array waveguides

Reference: Silica-on-silicon devices

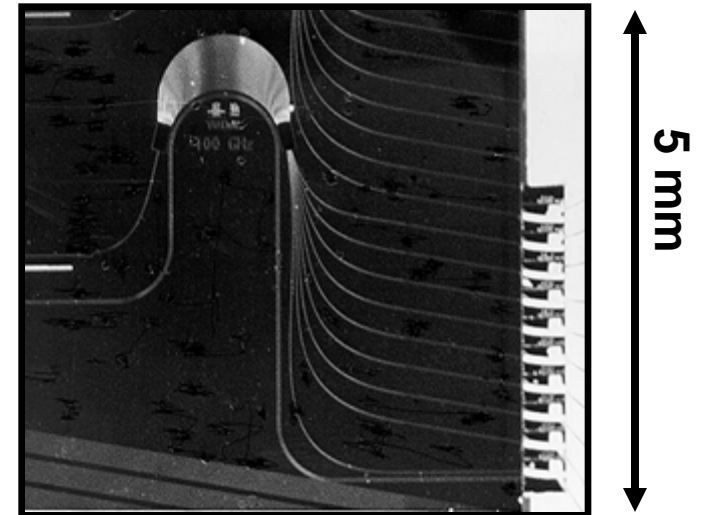


Size: Several square centimeter

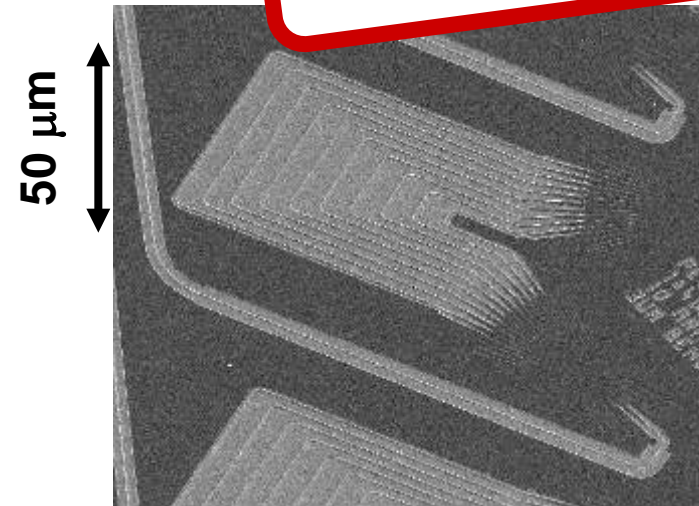


**Low Contrast - Fiber Matched
(silica or polymer based)
Bend Radius ~ 5 mm
Size ~ several cm²**

Density x 10⁶



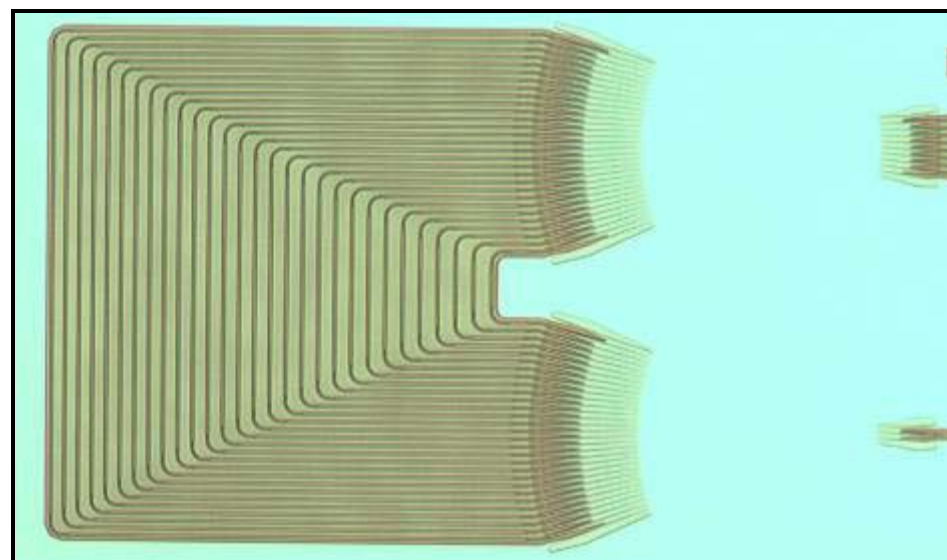
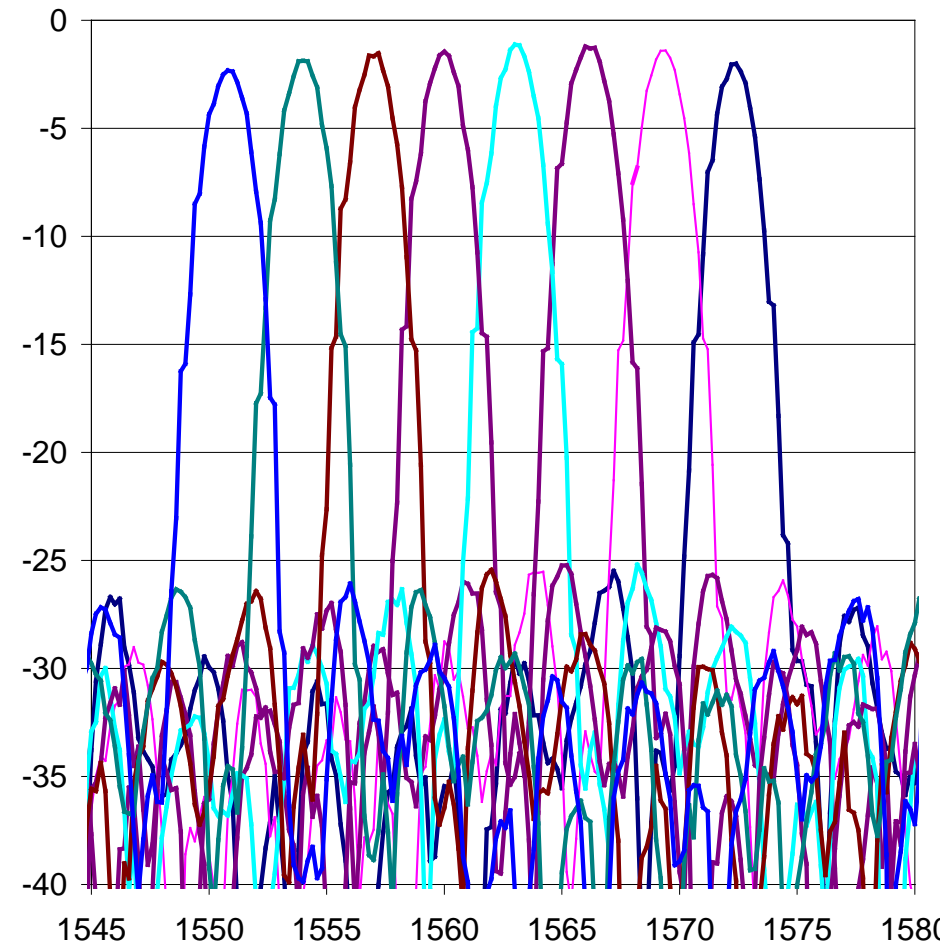
**Medium Contrast
(InP-InGaAsP)
Bend Radius ~ 500µm**



**Ultra-high Contrast
(Silicon on Insulator)
Bend Radius < 5µm**

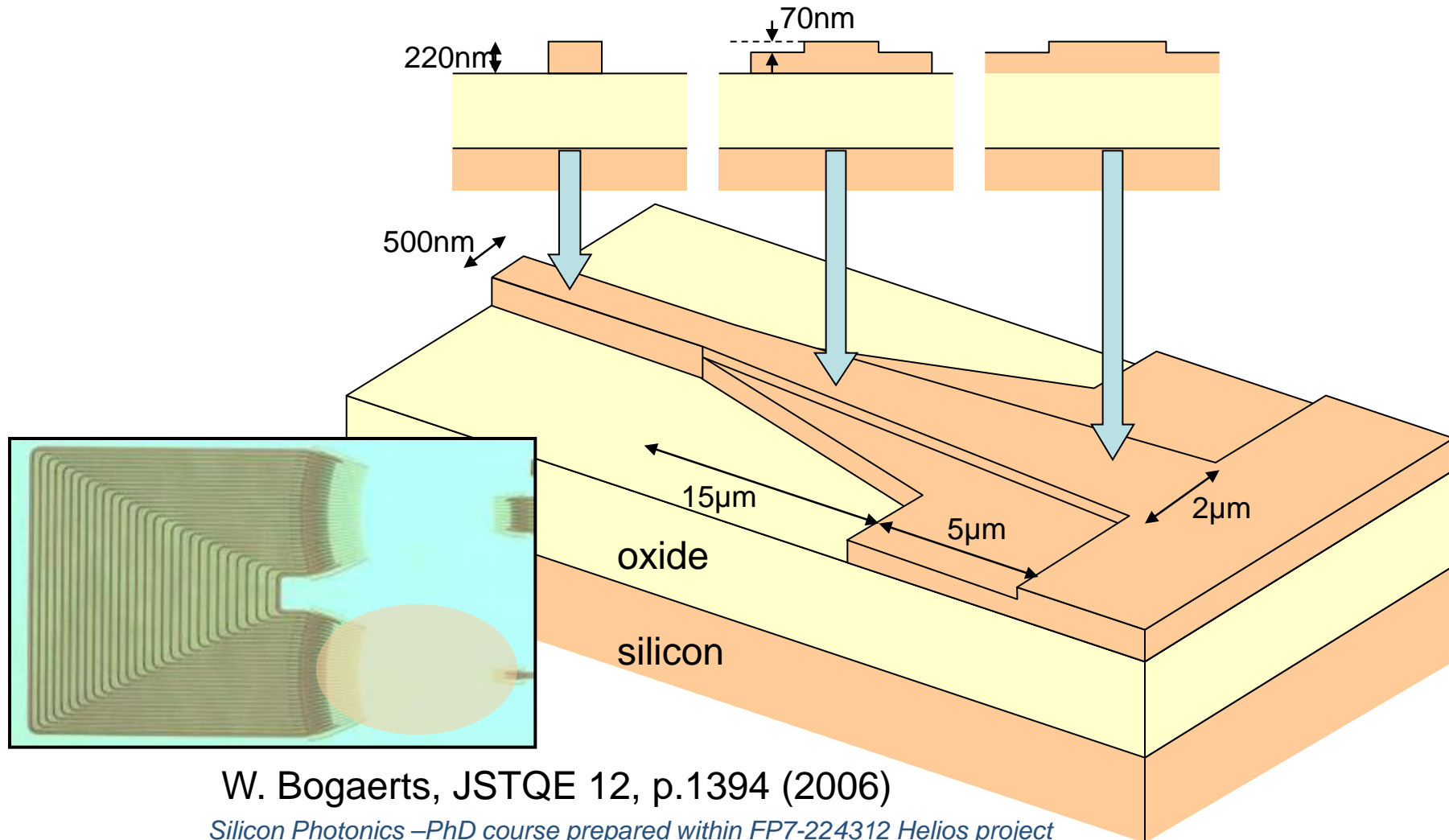
Arrayed Waveguide Grating

- 8-channel, 400GHz
- FSR = 30nm
- footprint = 200 x 350 μm^2
 - -25 dB crosstalk level
 - -1 dB insertion loss (center channel)
 - 1.5 dB non-uniformity

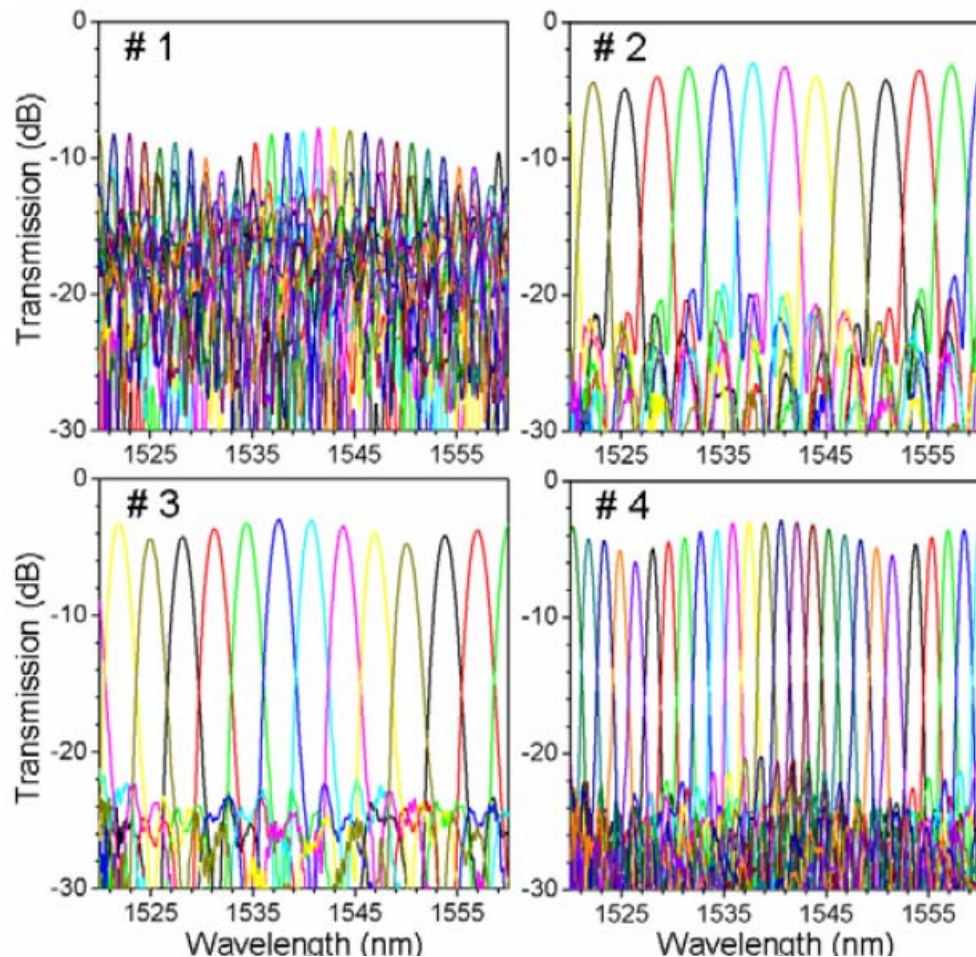
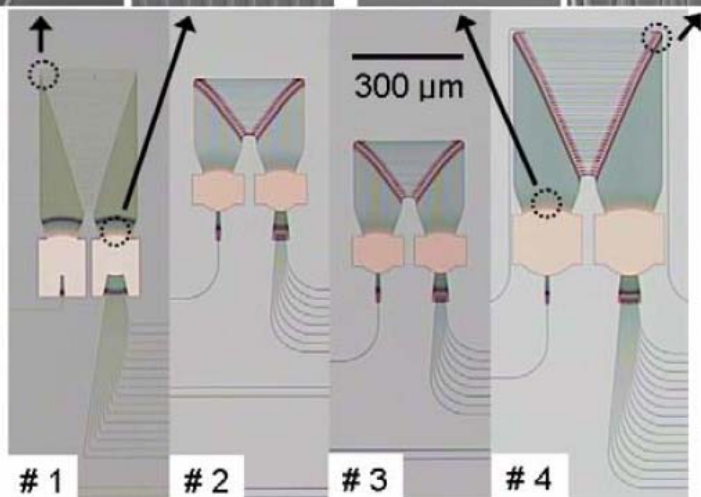
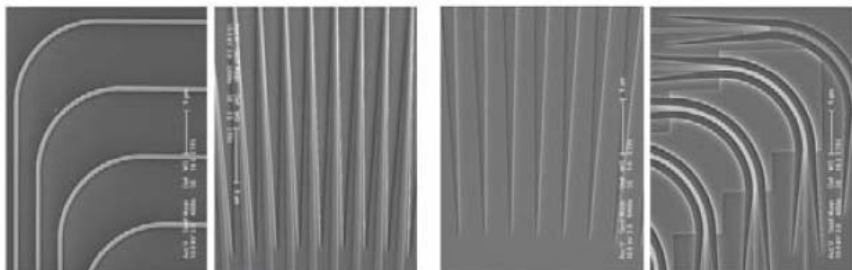


• Star coupler:

- shallow etch for less contrast



Use of shallowly etched waveguides for crosstalk reduction



DJ Kim e.a. PTL 20 (17-20) p 1615 (2008)

- Outline
 - The Straight Waveguide

**Basic components with high performance have been demonstrated using silicon wire waveguides
The next step is to combine them to realise more complex circuits**

- The Mach–Zehnder Interferometer
- The AWG